



Digital-X: DLR's Way Towards the Virtual Aircraft

Norbert Kroll, Cord Rossow

German Aerospace Center (DLR)

Institute of Aerodynamics and Flow Technology



Knowledge for Tomorrow

DLR (German Aerospace Center)

Fields of Research

Aeronautics



≈ 85% (activities, personnel, budget, funding)

- ~ 7000 employees
- 33 Institutes and facilities
- Turnover ca. 1.3 B€ (2010)
 - 745 M€ for research & development
 - **205 M€ for aeronautics**

Space



Energy



Transport



≈ 15% (activities, personnel, ...)

Defence&Security



Cross-Function,
Inputs from the
4 Programms

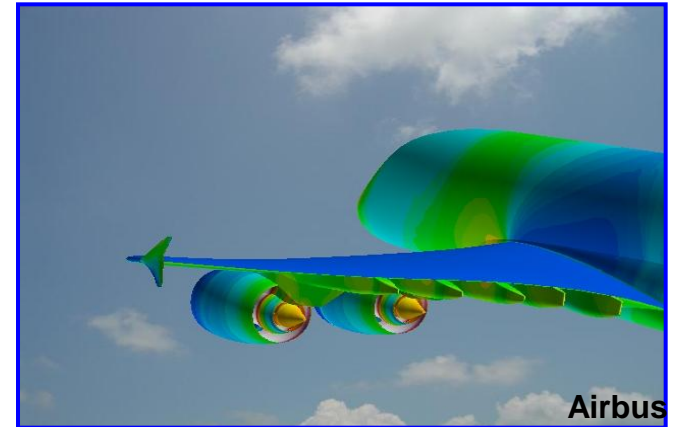
Plus:

- Space Administration
- Project Management Agency



Outline

- Background & Motivation
- DLR's Vision: Digital-X
 - Physical Modeling
 - CFD Solver
 - Full Flight Simulation
 - Multidisciplinary Optimization
- Summary



ACARE 2020 / Flightpath 2050

ACARE: Advisory Council for Aeronautics Research in Europe

Europe's Vision for Aviation

- Maintaining Global Leadership & Serving Society's Needs

Goals *(relative to typical aircraft in 2000)*

- CO₂ emissions reduced by 75%
- NOx emissions reduced by 90%
- 65% reduction in perceived aircraft noise



Consequence

- Heavy demands on future product performance
- Step changes in aircraft technology required
- New design principles mandatory



Numerical Simulation

Key Enabler for Future Aircraft Design

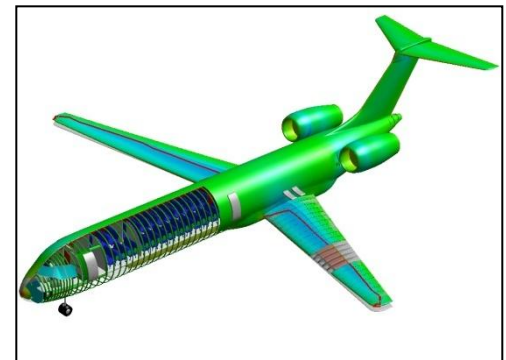
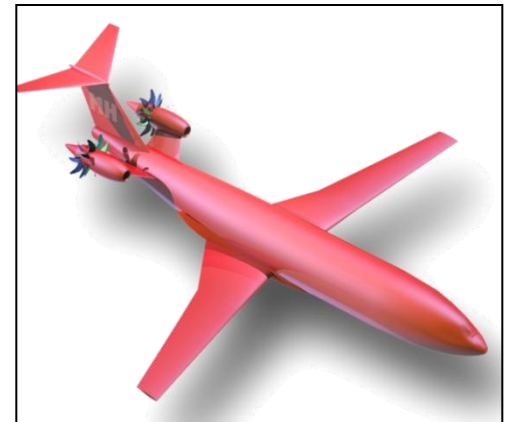
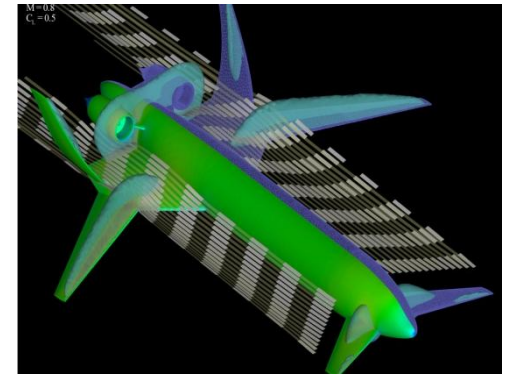
Future aircraft

- Design may be driven by unconventional layouts
- Flight characteristics may be dominated by non-linear effects

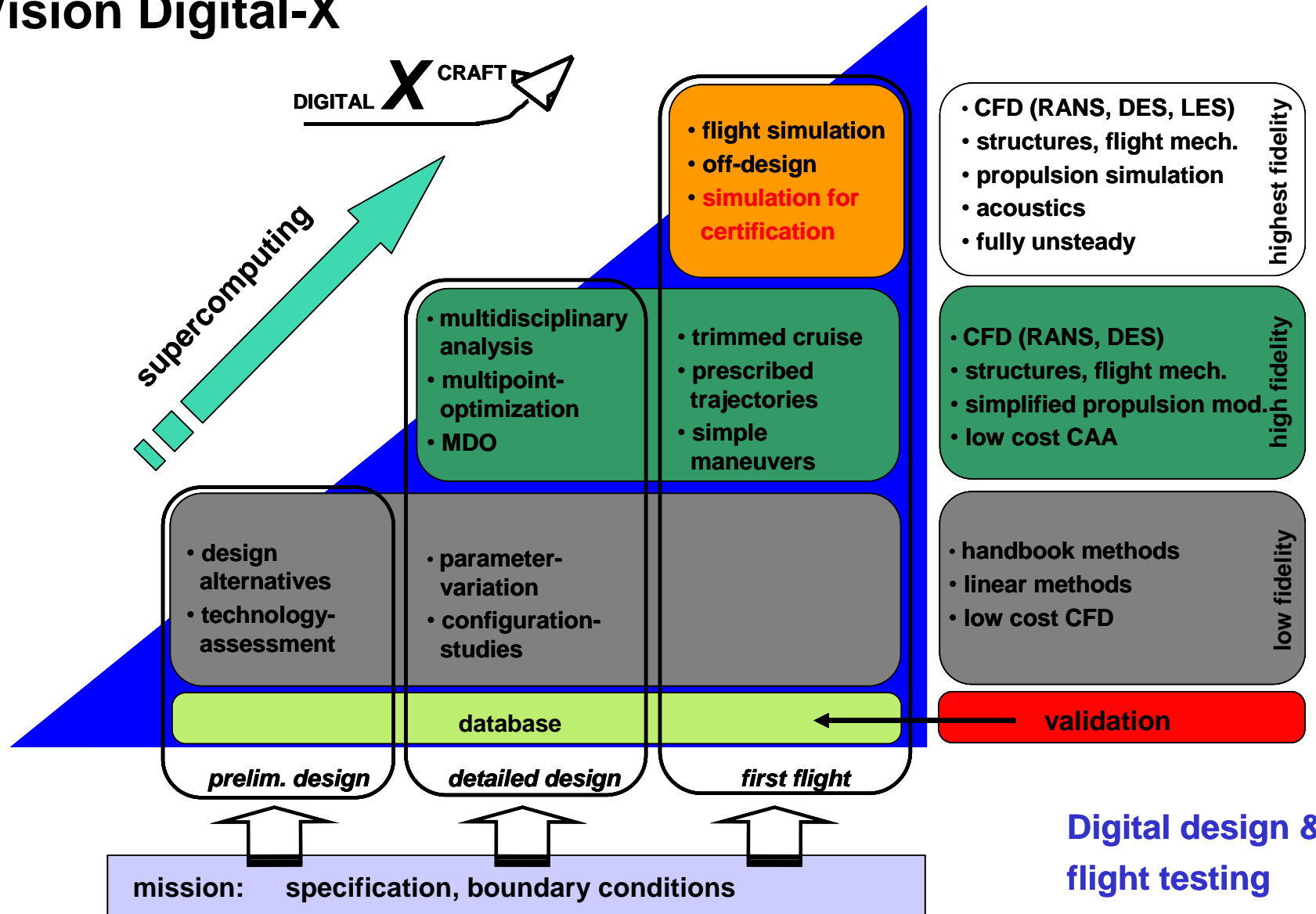
High-fidelity methods indispensable for design & assessment of step changing aircraft

- Reliable insight to new aircraft technologies
- Comprehensive sensitivity analysis with risk & uncertainty management
- Best overall aircraft performance through integrated aerodynamics / structures / systems design
- Consistent and harmonized aerodynamic and aero-elastic data across flight envelope

Further improvement of simulation capability necessary



Vision Digital-X



DLR Project Digital-X

Towards Virtual Aircraft Design and Flight Testing

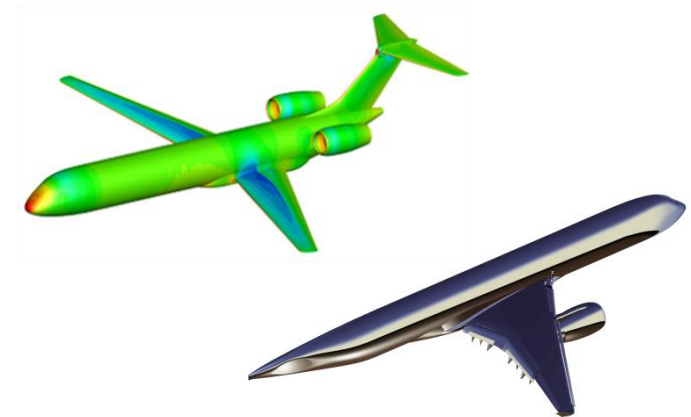


Long term goals

- Development of an integrated software platform for multi-disciplinary analysis & optimization based on high fidelity methods
 - Integration of relevant disciplines

Short term goals (1st phase 2012-2015)

- Prototype of integrated software platform
- Demonstration of new capabilities using industrial relevant configurations



Main activities

- CFD solver improvement, reduced order modeling, maneuver simulation, MDO, uncertainty quantification, parallel simulation environment

Project partners

- 9 DLR institutes, Airbus associated partner
- Strong links to national research projects (*Federal Aeronautical Research Programme*) (*Cassidian, RRD, ECD, Universities of Braunschweig, Stuttgart, Aachen, Darmstadt, München, ..*)



DLR Project Digital-X

Towards Virtual Aircraft Design and Flight Testing

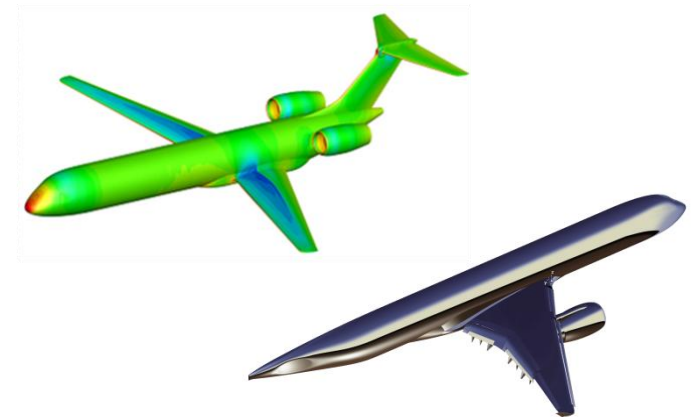


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- **CFD solver improvement**, reduced order modeling, **maneuver simulation**, **MDO**, uncertainty quantification, parallel simulation environment

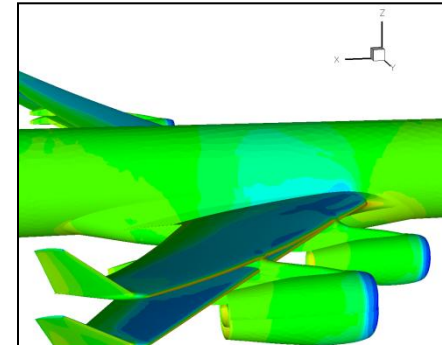
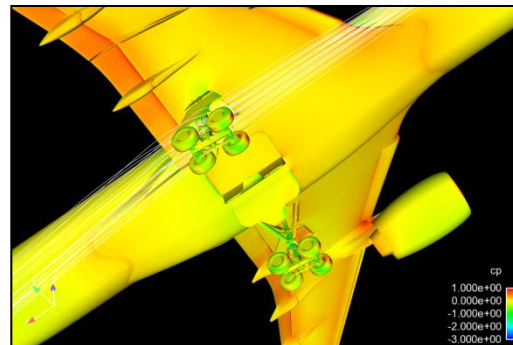
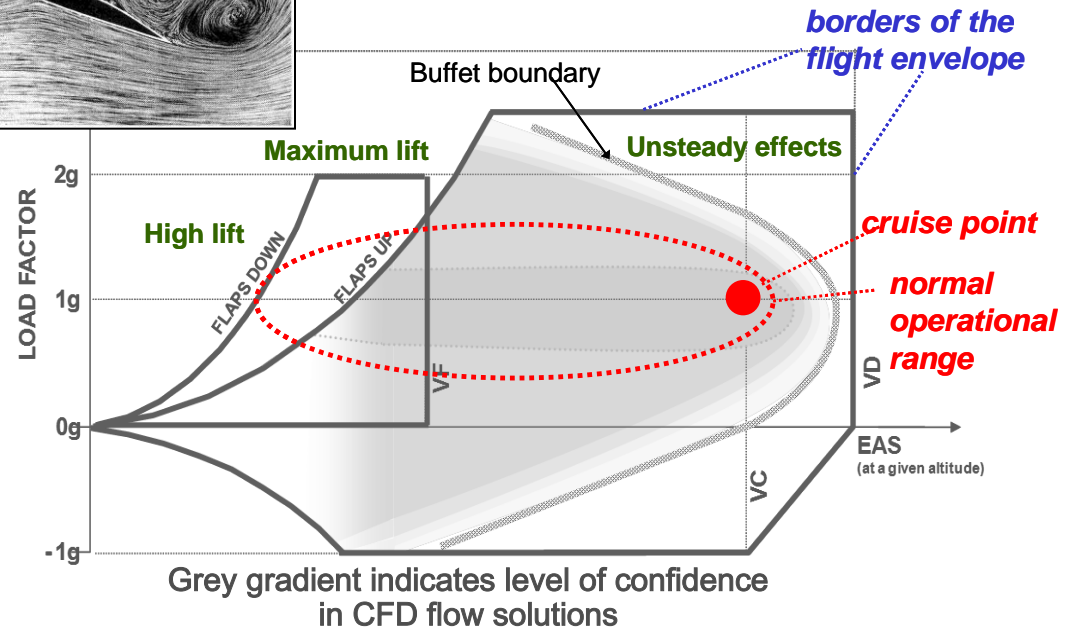
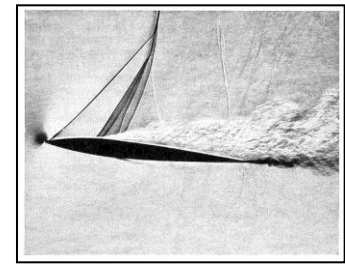
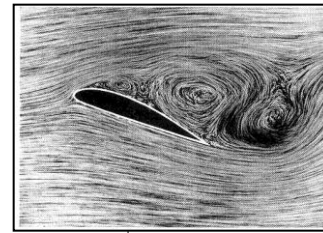
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Digital Aircraft Challenges

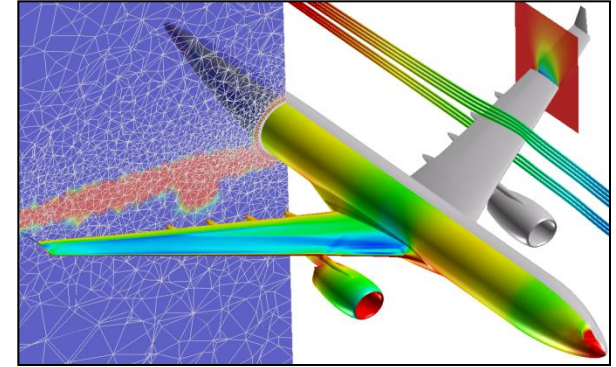
- Simulation of full flight envelope
- Physical modeling of flows with separation
- Reliable & efficient CFD computations
 - Complete A/C
 - Complex flows
 - Huge number of cases (CFD for data)
 - Unsteady computations
- Coupling of all relevant aircraft disciplines
 - Maneuver simulation
 - Loads prediction
- Multi-disciplinary optimization



DLR CFD Codes

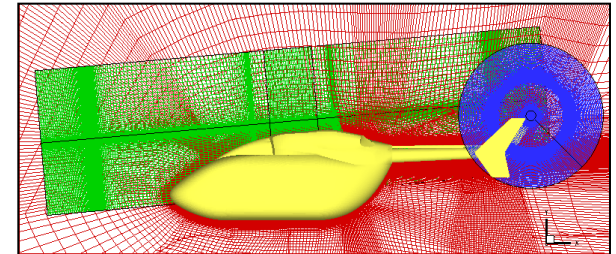
TAU-Code (*Production code*)

- Unstructured hybrid meshes, overlapping grids
- RANS, hybrid RANS/LES
- Edge-based 2nd-order FV solver
- Grid re- & de-refinement
- Linear and adjoint solver
- Hybersonic extension
- Incompressible version THETA



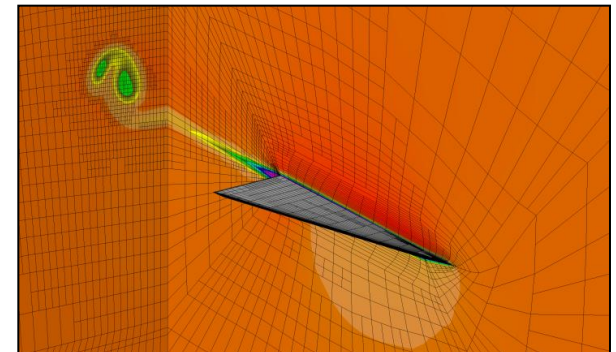
FLOWer-Code (*For dedicated applications*)

- Block-structured 2nd-order FV solver
- Overlapping grids



PADGE-Code (*Research Code*)

- Higher-order DG solver
- Unstructured mixed-element grids
- Isotropic & anisotropic hp-adaptation
- Reliable error estimator

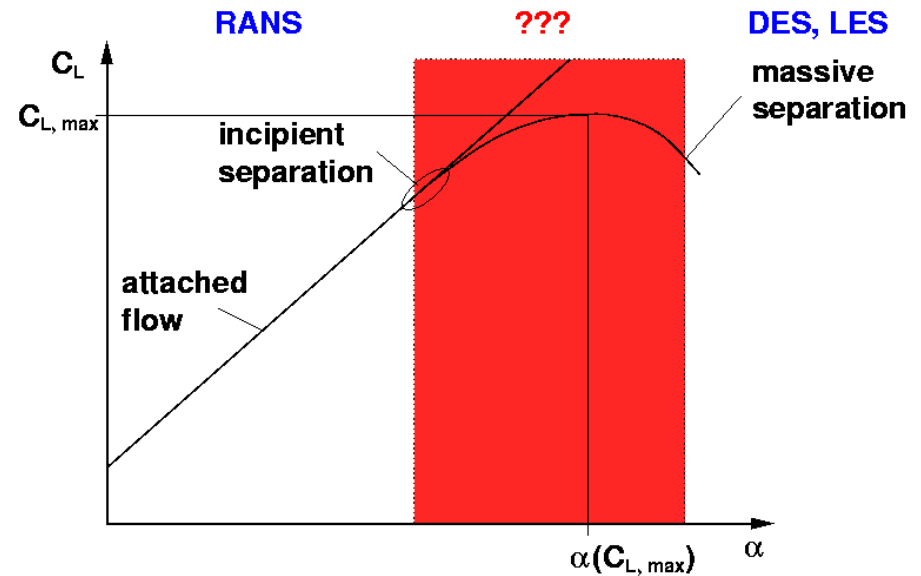


Physical Modeling

Challenge & Vision

CFD for off-design conditions

- Separation onset
- URANS vs. scale resolution
- Influence of transition



Vision: Unified model based on Reynolds Stress Transport for full flight envelope

- For macroscopically steady & unsteady flows
- Effects of favorable and adverse pressure gradients on turbulence to be included
- Wide range of applicability (separation, free vortices)
- Automatic switch from URANS to scale resolving method, in cases where details of turbulent spectrum relevant
- Correct behavior at turbulence onset

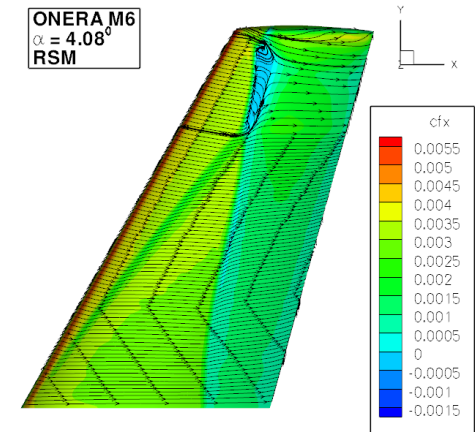


Physical Modeling

Current Status (TAU-Code)

Differential Reynolds Stress Models (RANS)

- SSG/LRR- ω model
 - „Simple“ standard model
 - Based on BSL ω -equation (Menter)



Standard RSM in TAU

EU-Project FLOMANIA

- **S**peziale-**S**arkar-**G**atski model (SSG) as common model chosen
- SSG model relies on length scale variable ε

Aerodynamics

- Length scale variable ω is advantageous

Reynolds stress model based on ω

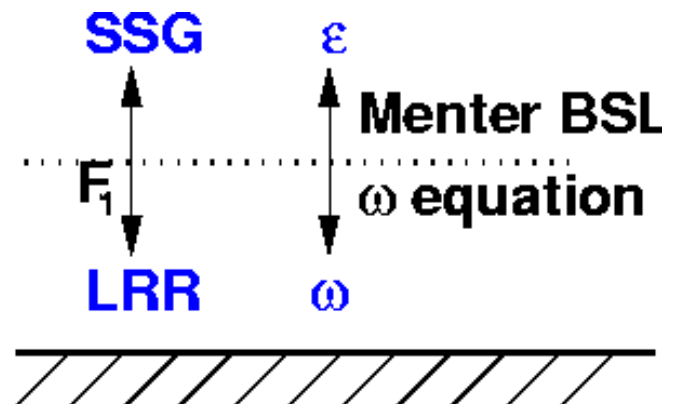
- Stress- ω model by Wilcox
= **L**aunder-**R**eece-**R**odi model (LRR) without wall reflexion

Idea:

- Model combination by coefficient blending (according to Menter models)

⇒ **SSG/LRR- ω model**

- Far field: SSG + ε
- Near wall: LRR + ω
- Coefficients:
Blending function F_1 by Menter
- BSL- ω -equation by Menter



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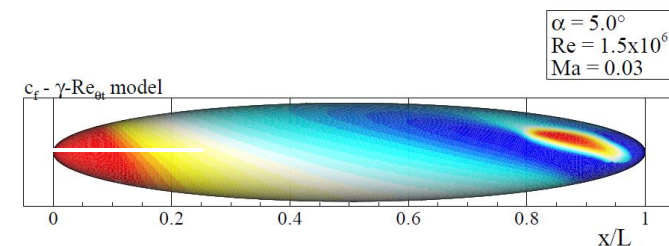
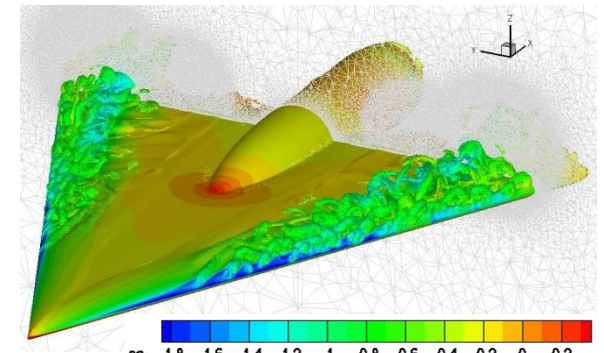
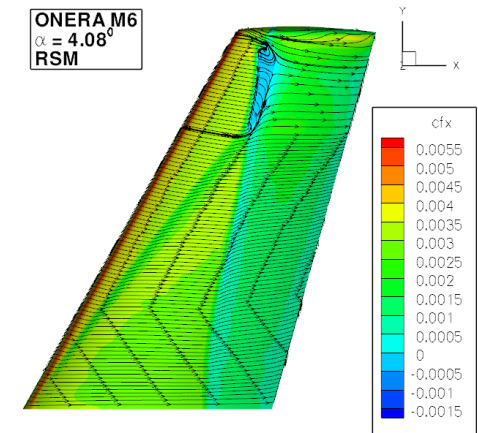
- SSG/LRR- ω model
 - „Simple“ standard model
 - Based on BSL ω -equation (Menter)
- JHh-v2 (Jakirlic-Hanjalic)
 - Advanced near-wall treatment
 - Based on homogeneous dissipation rate ε^h
 - Anisotropic dissipation

Scale resolving approaches

- DES (+ variants)
 - Based on various models
- Advanced URANS (SAS, PANS)
 - Based on SST model

Transition prediction

- e^N method
- Transport equation based model

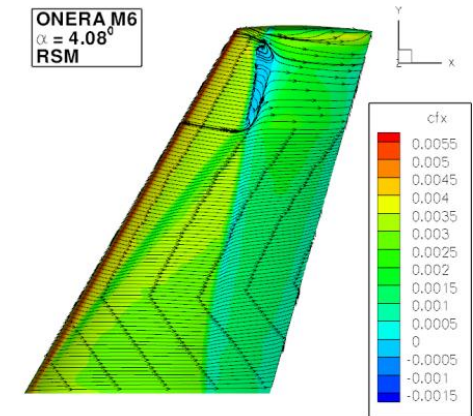
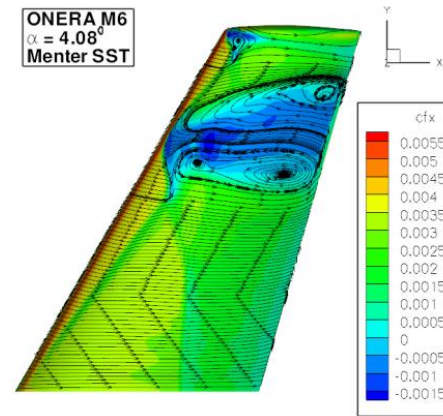
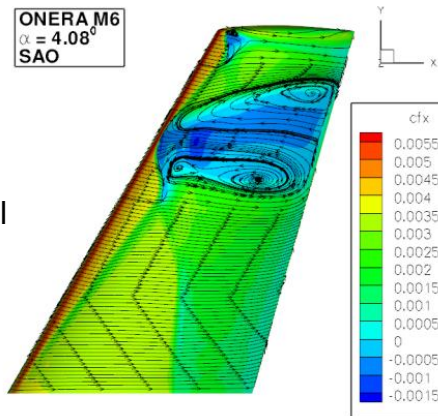
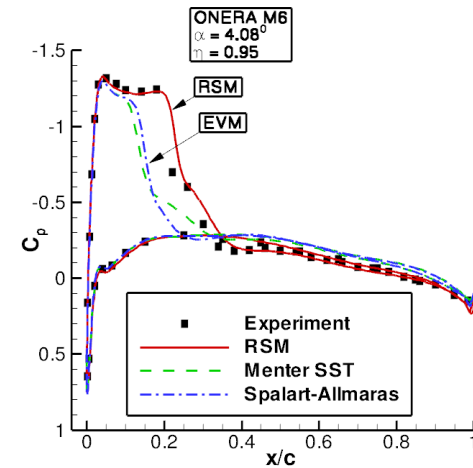
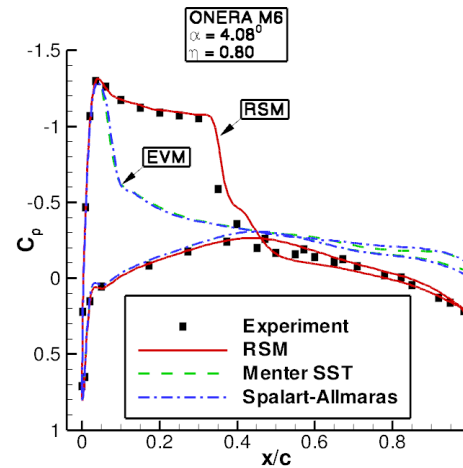
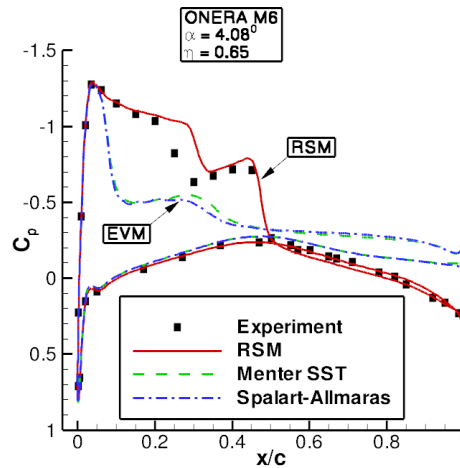


Turbulence Modeling

Application of Reynolds Stress Models to High-Speed Flow

ONERA M6 wing

- Shock-induced separation
- RSM delivers significantly better results compared to eddy viscosity models (EVM)



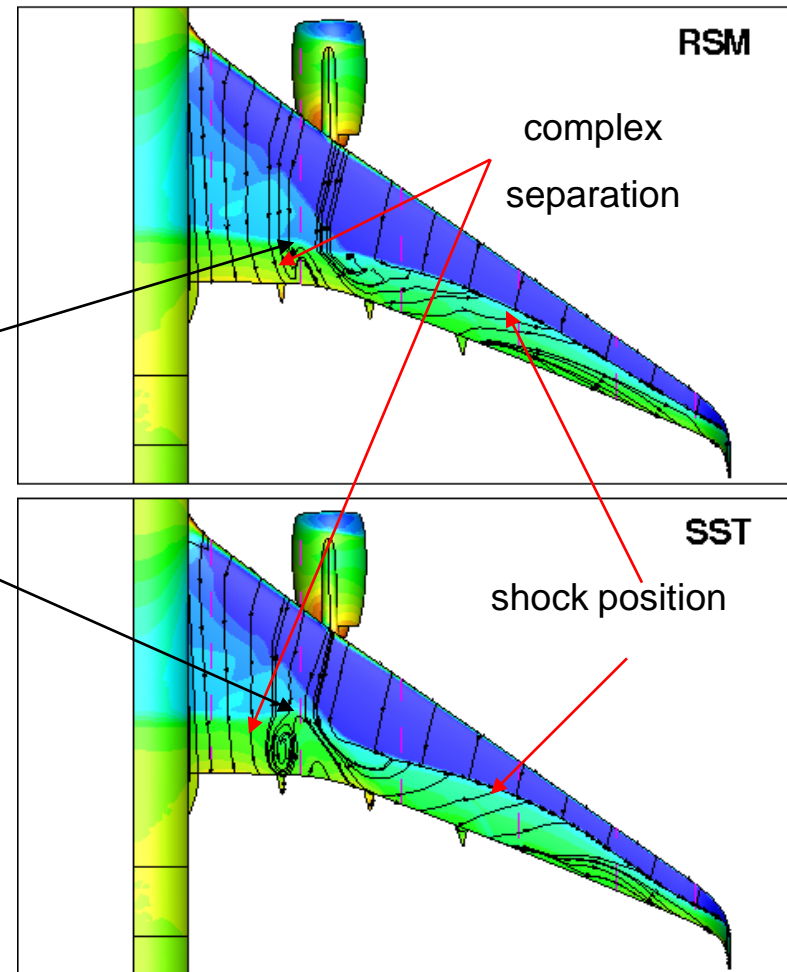
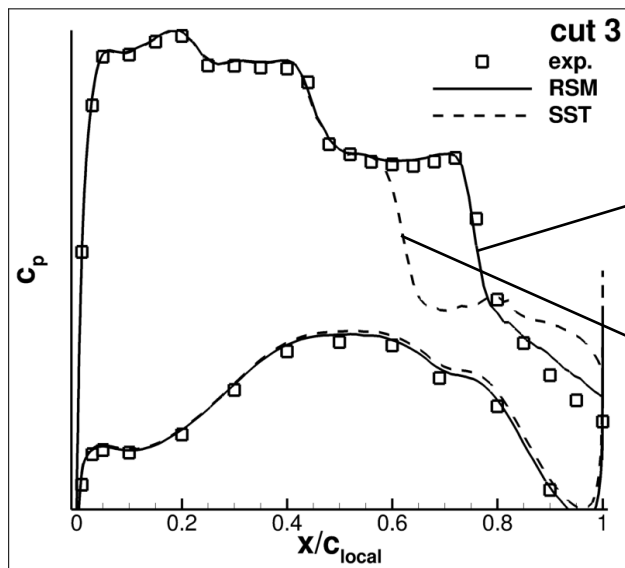
RSM: Reynolds Stress model
EVM: Eddy viscosity model



Turbulence Modeling

Application of Reynolds Stress Models to High-Speed Flow

Complex separation (transport aircraft)

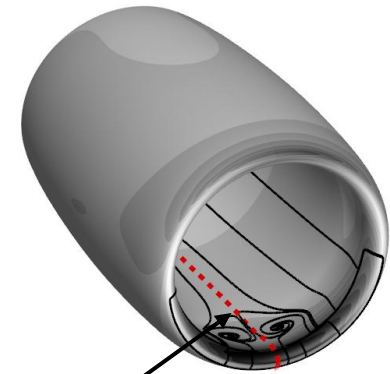


Turbulence Modeling

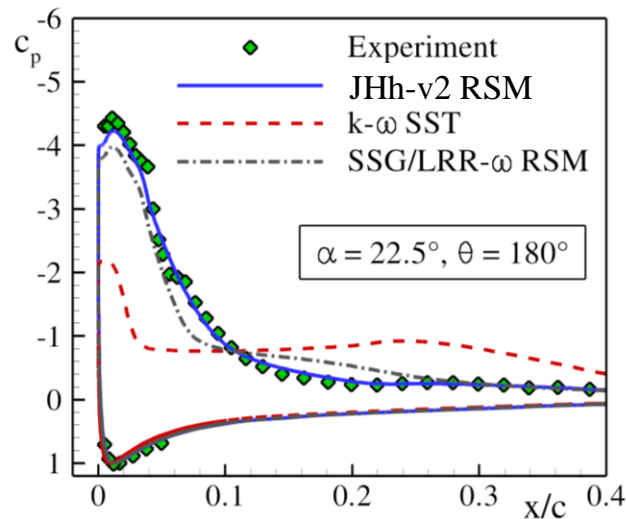
Application of Reynolds Stress Models

Stall characteristics (nacelle)

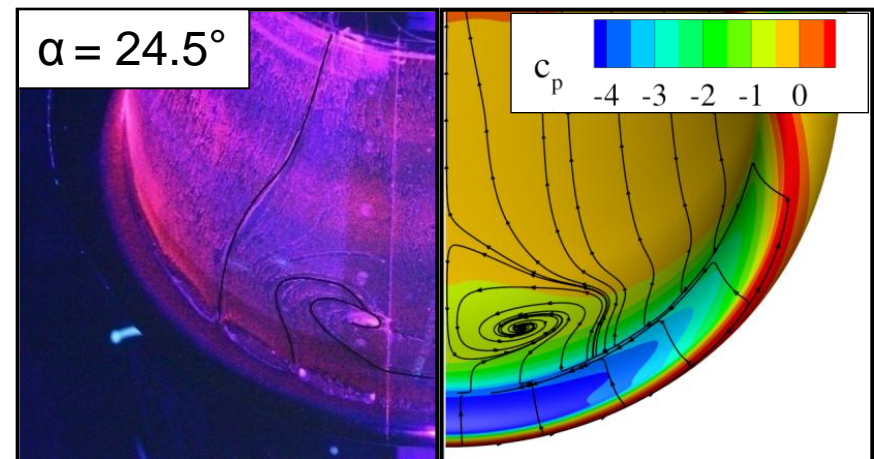
- $M = 0.15$, $Re = 1.3$ million
- URANS combined with e^N method
- Measured separation onset around $\alpha \geq 24^\circ$
- Improvement by DRSM, in particular JHh-v2



$\theta = 180^\circ$



Surface pressure in inlet symmetry plane



Oil-flow picture (left) and JHh-v2 RSM (right)

Physical Modeling

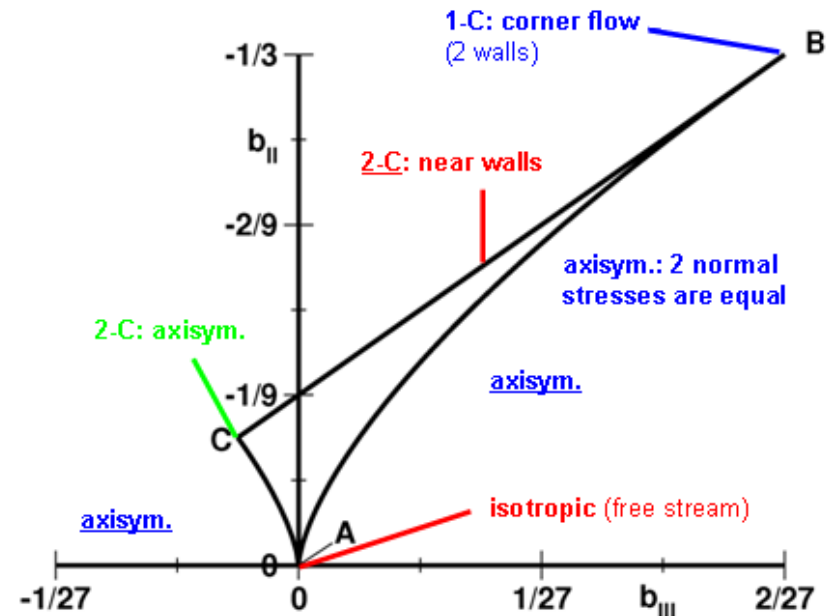
Activities / Perspectives - DRSM

Fundamental investigations

- Near-wall flow physics
- Effect of positive pressure gradients

Improved Reynolds Stress Modeling

- Non-linear re-distribution modeling
 - Analysis of physical constraints
 - Hierarchy in complexity
- Anisotropic dissipation modeling
 - Analysis of physical constraints
 - Focus on near-wall region
- Compressibility effects
 - Analysis of flow equations
 - Transfer of modeling principles
- Length scale equation
 - Maintain boundary layer characteristics
 - Enhance sensitivity to separation



Invariant map allows

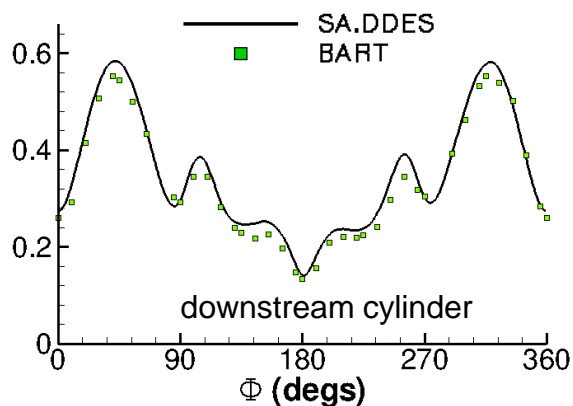
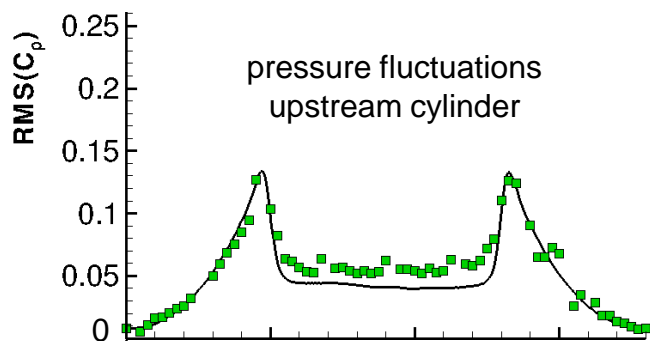
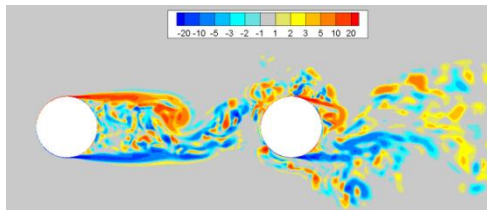
- Systematic analysis of RSM
- Reduction of free parameters



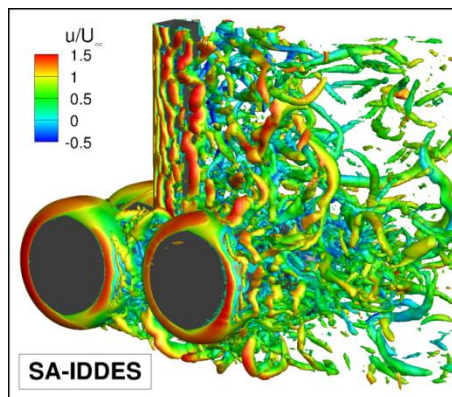
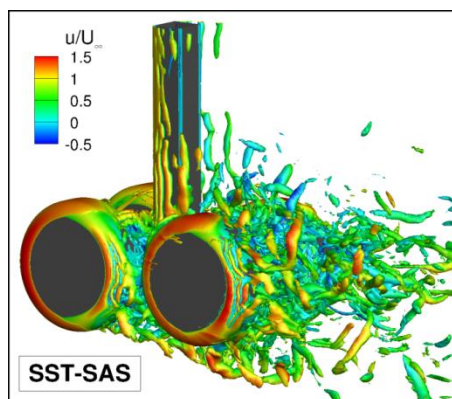
Turbulence Modeling

Status - Hybrid RANS/LES

Tandem cylinder (TAU-Code)

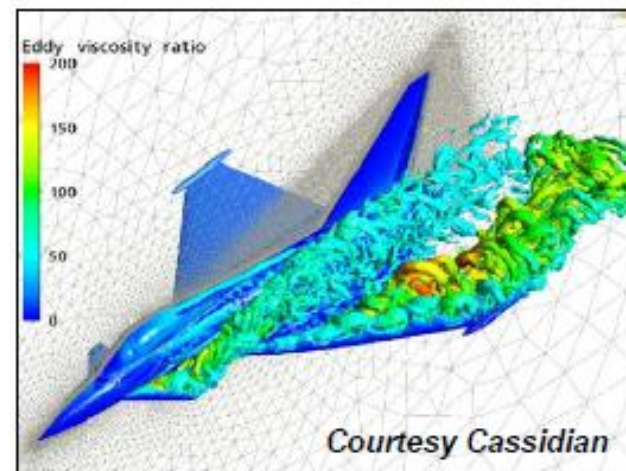


Simplified landing gear



DLR THETA-Code

FA-5 generic fighter at $\alpha=15^\circ$



EU project DESider, Springer book, 2009

DLR TAU-Code

**Improvements required
for prediction of
incipient separation**



Physical Modeling

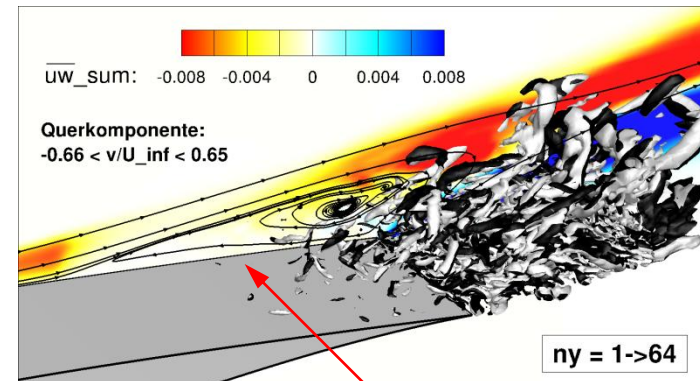
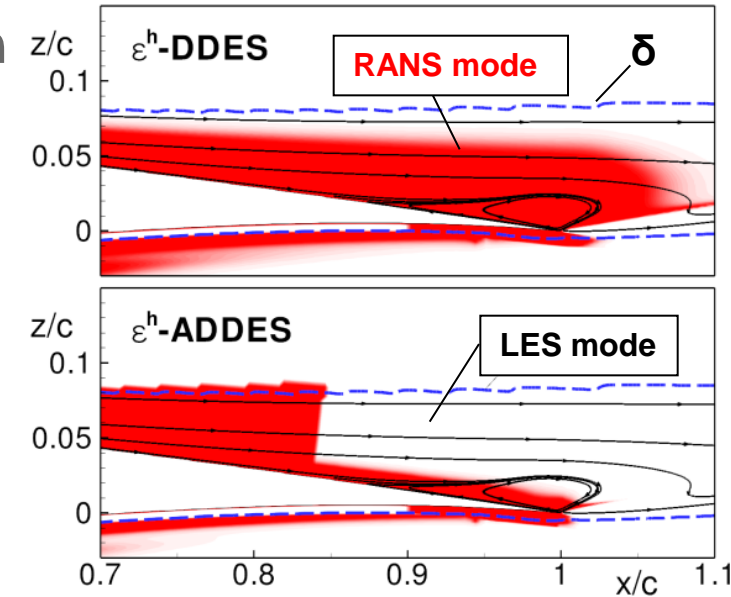
Activities / Perspectives - Scale Resolution

DRSM extension to scale resolution

- Coupling of existing approaches (*DES/DDES/IDDES, SAS, PANS*) with DRSM
- Onset of scale resolution
 - Definition of criteria (ADDES) (RANS/LES sensors based on boundary layer quantities)
 - Physical based forcing of fluctuations

LES

- Focus on studies concerning
 - Structured/unstructured grids
 - 2nd-order/high-order methods



NO break-up into small scale structures above the surface at shallow separation

No forcing of fluctuations applied

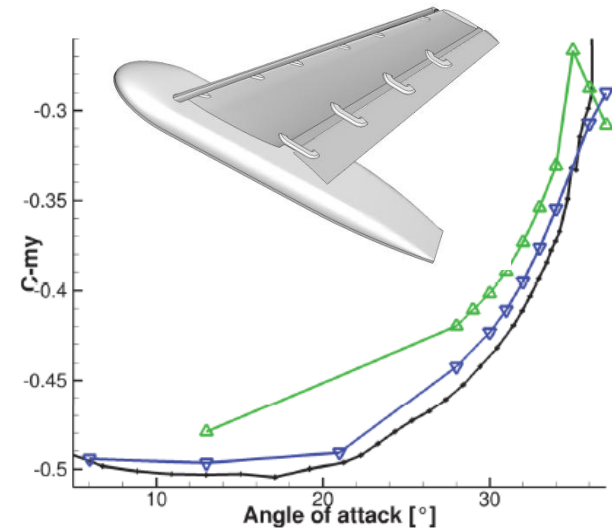
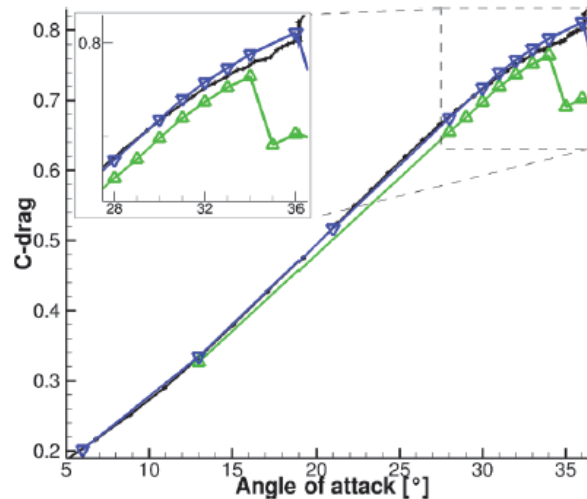
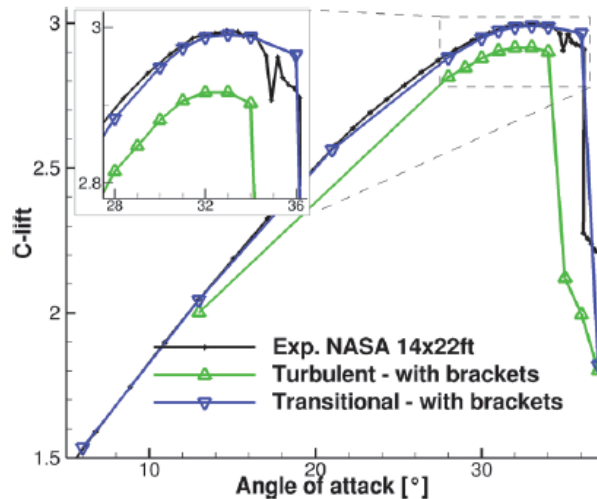
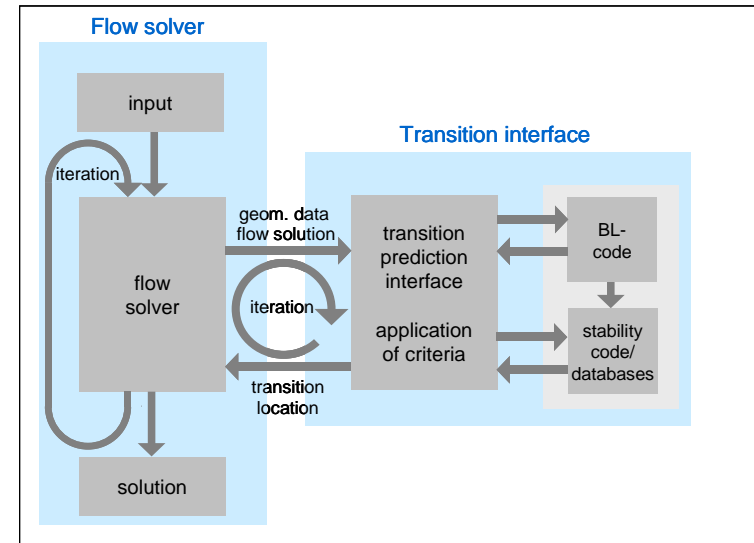


Transition Prediction

Status - e^N Method

NASA TRAP Wing

- $M = 0.2$, $Re = 4.3 \cdot 10^6$, $\alpha = 6^\circ - 36^\circ$
- $NTS = 8.5$, $NCF = 8.5$
- Transitional computations result in proper prediction of
 - Pitching moment
 - Stall characteristics



Physical Modeling

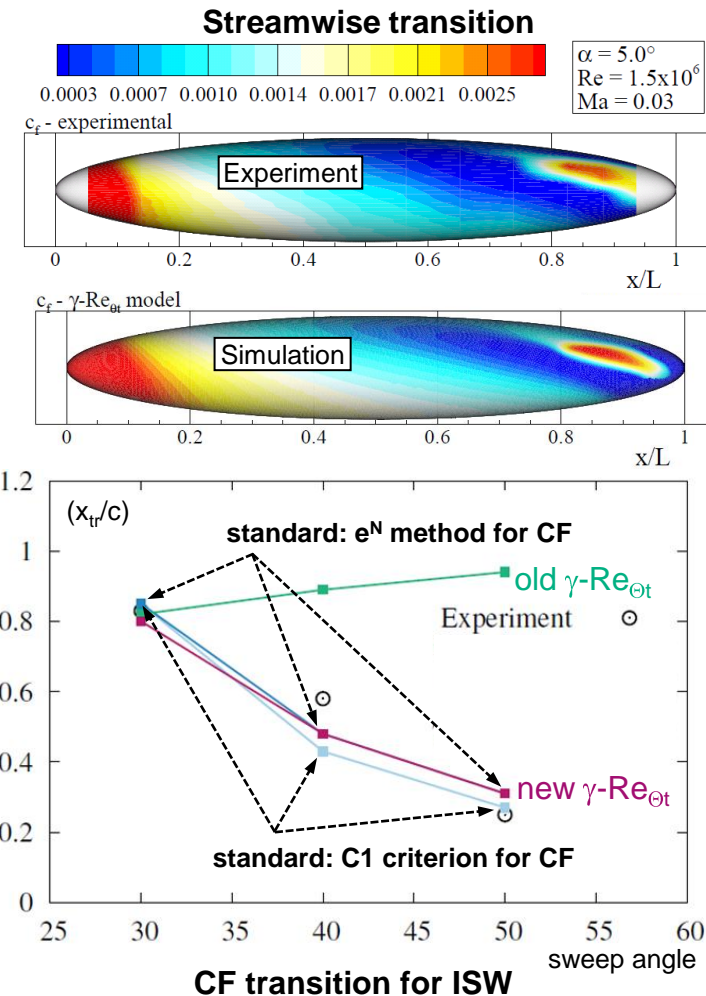
Activities / Perspectives – Transition Prediction

Correlation-based transition model $\gamma\text{-Re}_{\Theta t}$

- Integral part of a flow solver
- Good results for a variety of flows dominated by streamwise transition mechanisms (2D+3D)
- Potential to be extended to flows dominated by Cross-Flow (CF) transition
- Potential for using transition prediction in adjoint-based optimization

Planned Activities

- Extension to CF instabilities on arbitrary 3D wings
- Calibration of the model functions, validation



CFD Solver

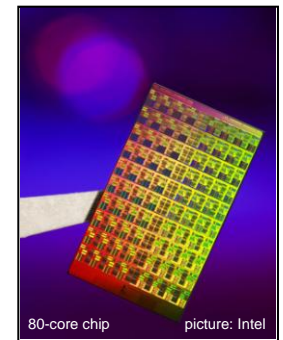
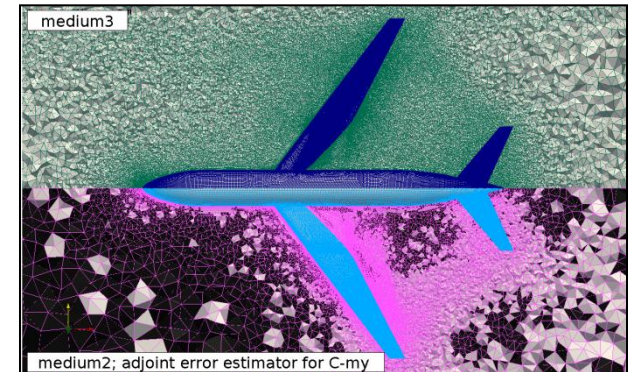
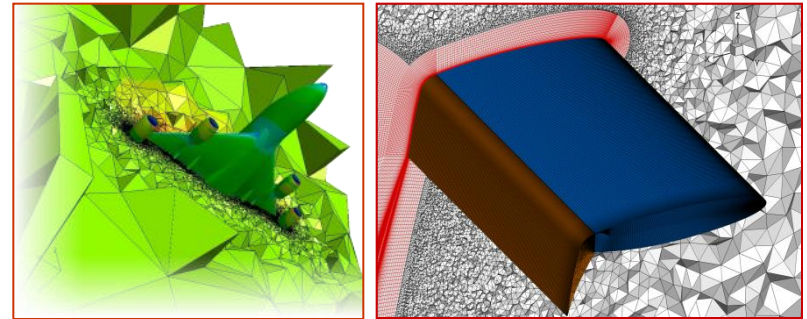
Challenge

- Accurate, efficient and robust / reliable solver for a given physical model

Aspects / issues

- Grid generation
- Adaptive mesh refinement
- Discretization issues
- Solution strategies
- Adaptation to novel hardware technique

Goal: Layout and prototype realization of Next Generation Solver



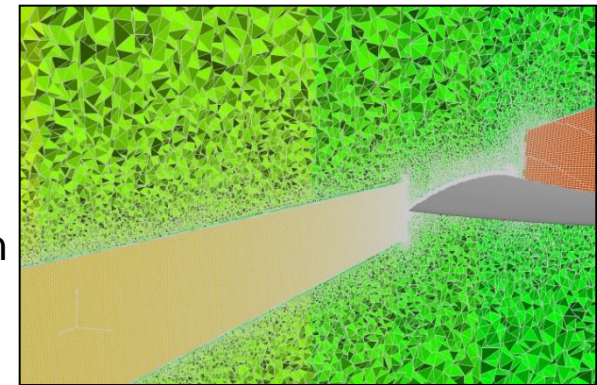
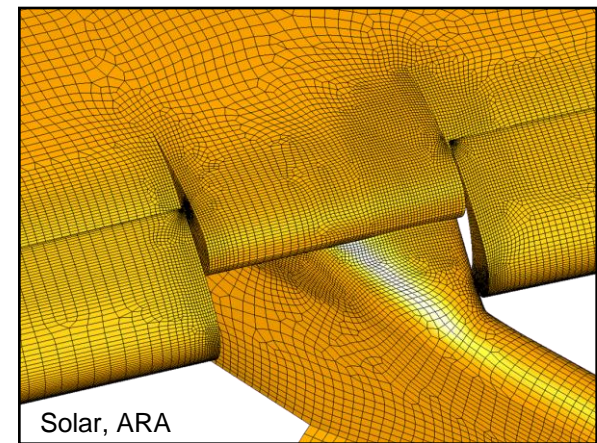
Grid Generation (Unstructured)

Requirement

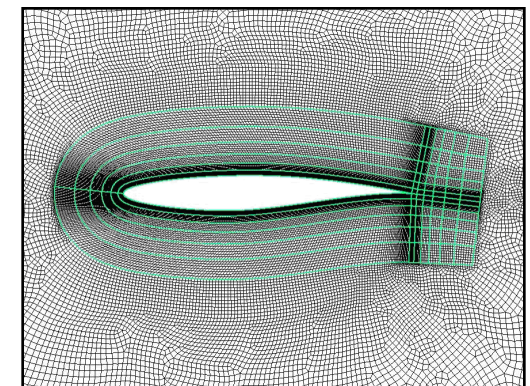
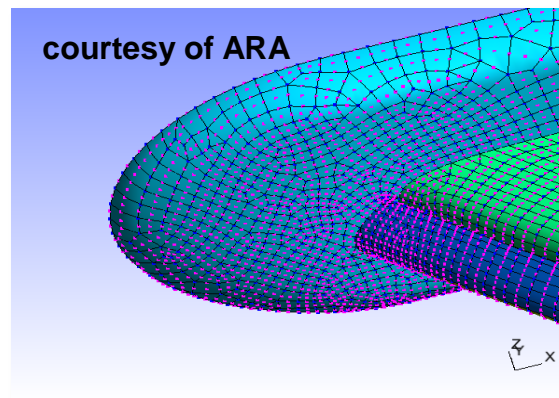
- Direct control of grid quality for unstructured grids

Vision

- Hex-dominant unstructured meshes
- Physical anisotropies reflected in mesh topology (boundary layers, high aspect ratio wings, rotor blades)
- Adapted wake and vortex resolution
- Cartesian mesh regions for general flow field resolution
- Support for overlapping mesh components (movables)
- Higher-order boundary representation



Centaur



Hyperflex mesher, courtesy of Airbus



Grid Generation (Unstructured)

Requirement

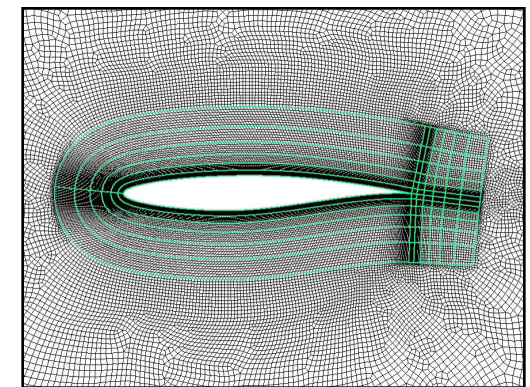
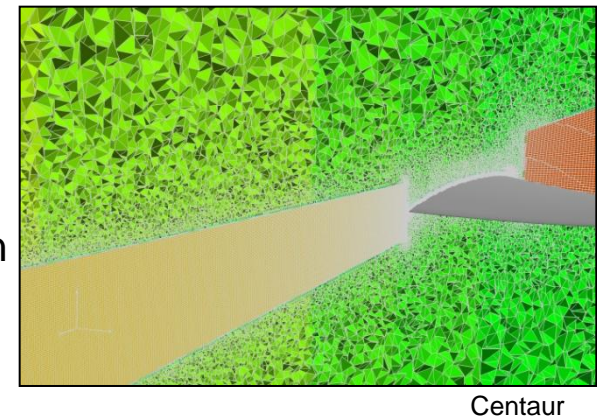
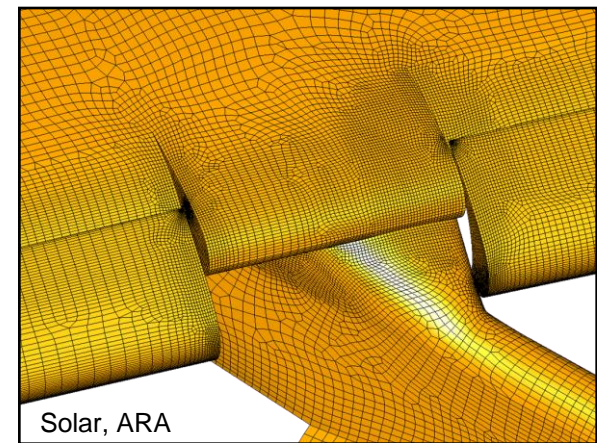
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Approach

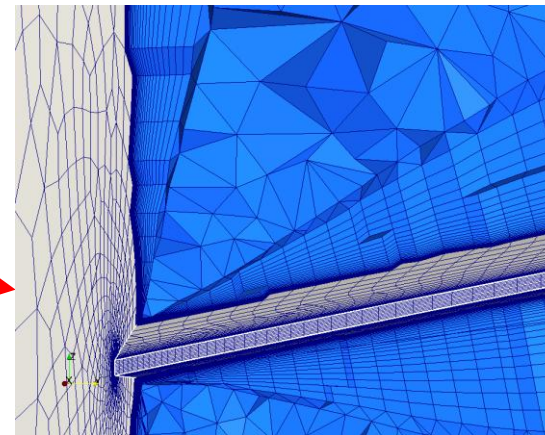
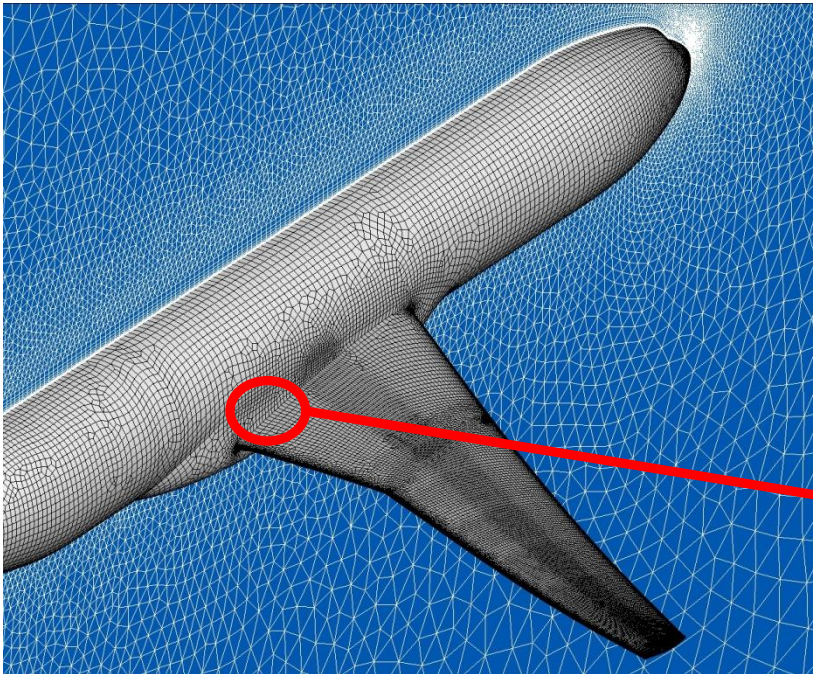
- Extensive evaluation of available software
- No major grid generation activities at DLR
- Co-operation with grid generation software vendors
 - Centaur (Centaursoft)
 - SOLAR / Hyperflex mesher (ARA/Airbus)



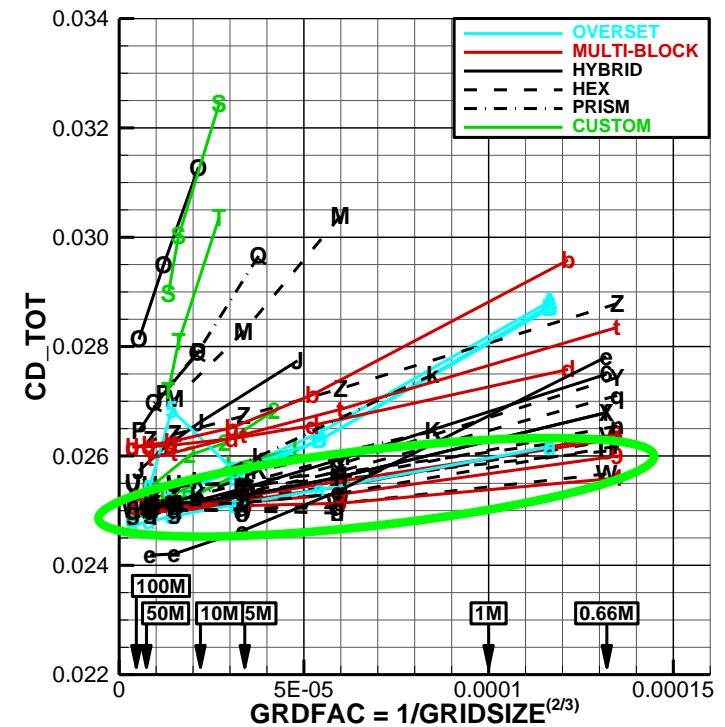
Grid Generation

Status / Current situation

- Hex-dominant grid families can deliver grid convergence similar to fully structured grids
- Limitations of adequate element quality in concave areas



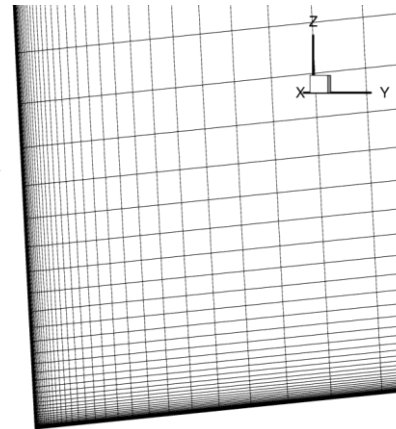
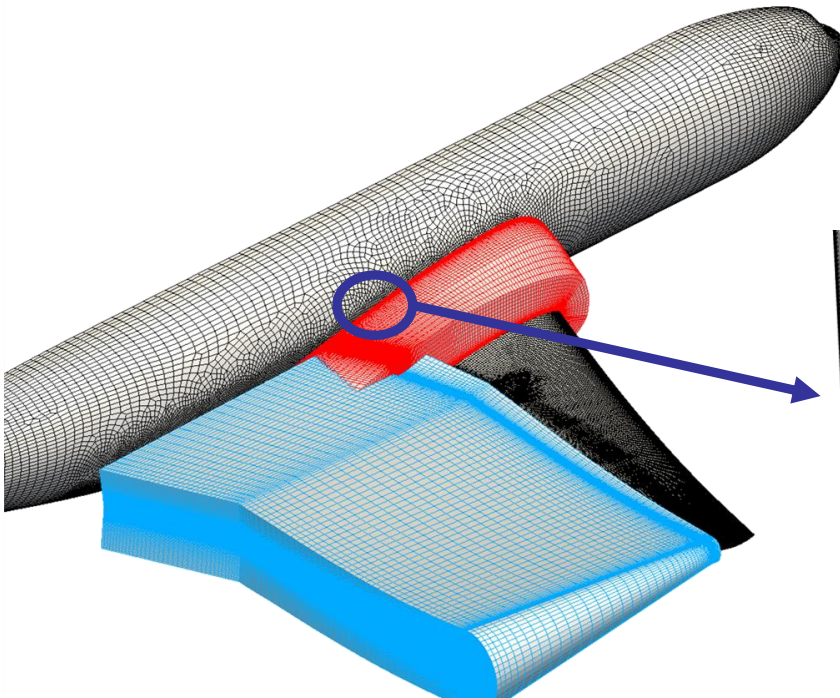
Wing Fuselage Corner
initial hex-dominant grid



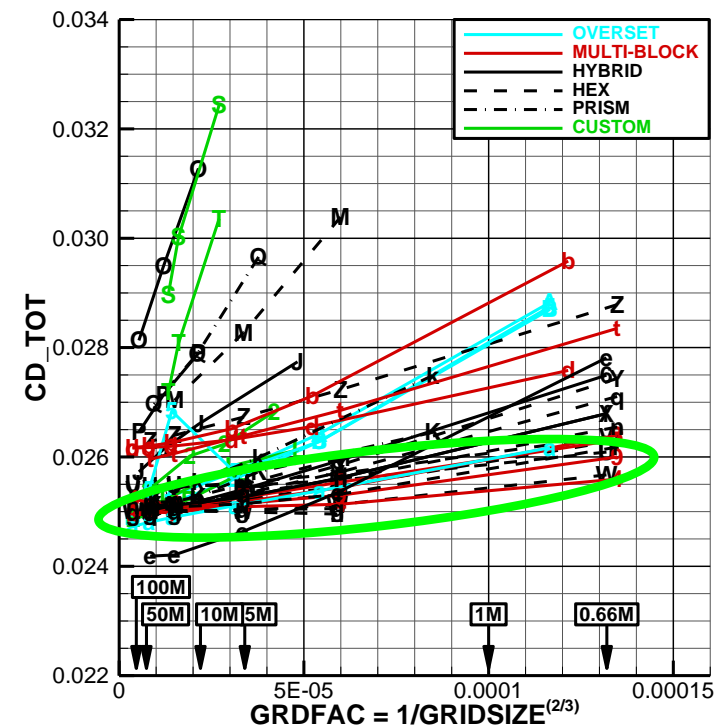
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Wing Fuselage Corner
overlapping block



CFD Solver

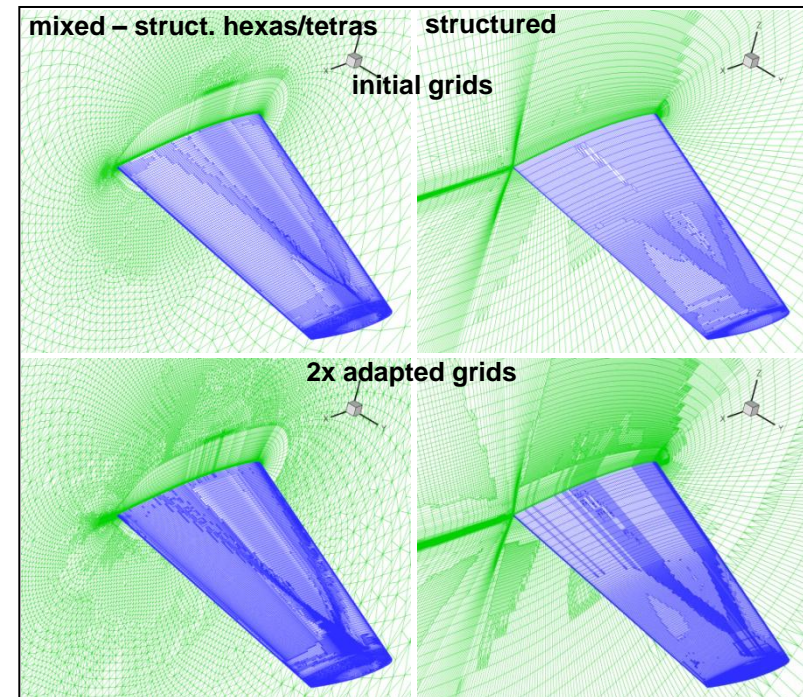
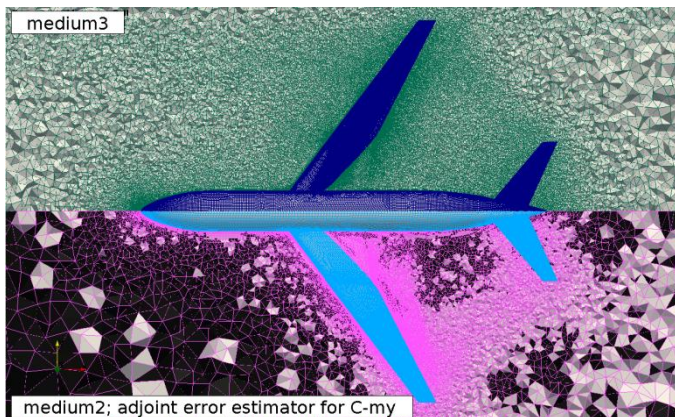
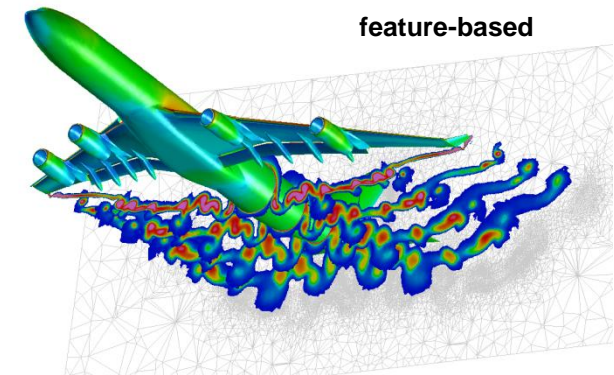
Adaptive Mesh Refinement

Status TAU-Code

- Local re- & de-refinement of mixed meshes
- Feature-based & goal-oriented indicator
- Parallel implementation (MPI)

Open issues

- Grid refinement strategies retaining structured grid regions
- Isotropic element refinement in structured boundary layers
- Industrialization for turbulent flows around complex configurations
- Adjoint adaptation for unsteady applications

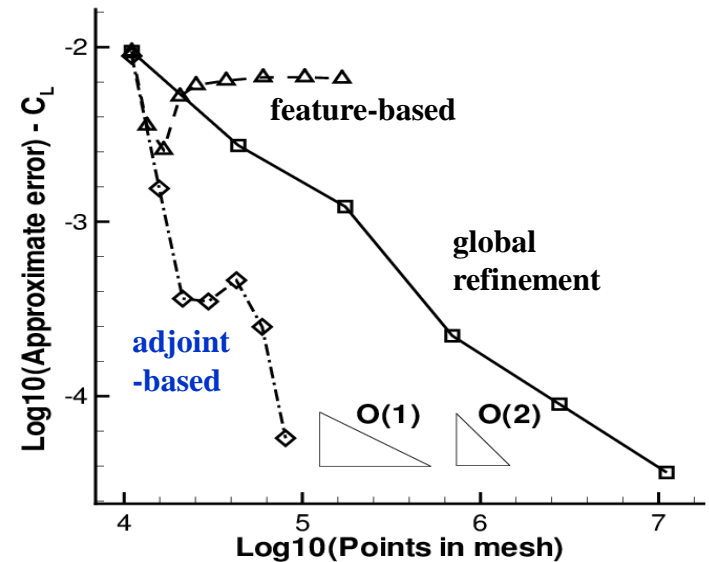
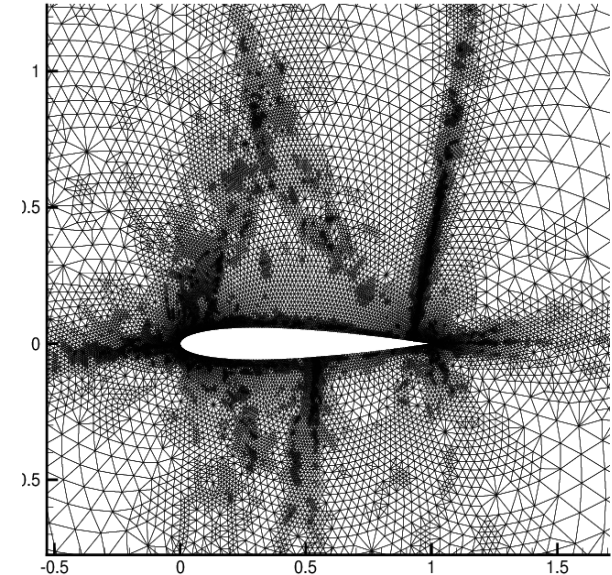
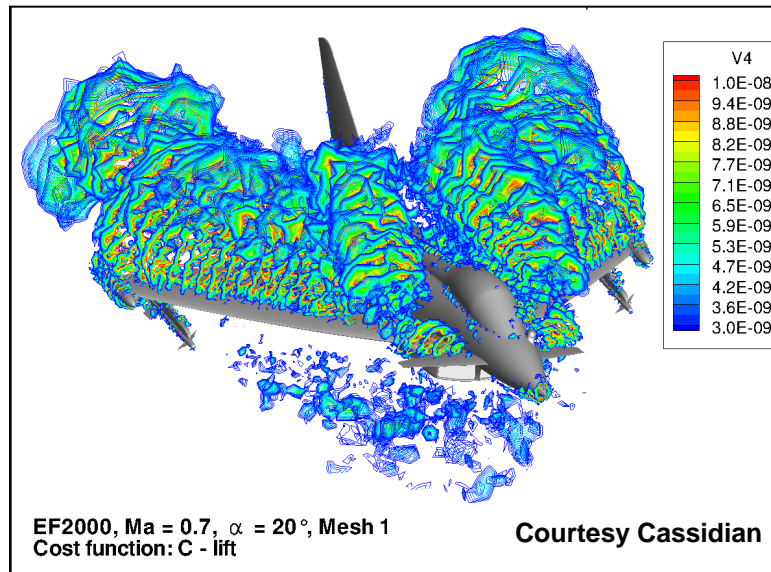


CFD Solver

Adaptive Mesh Refinement

Status TAU – Adjoint-based adaptation

- Measure sensitivity of dissipation based error on aerodynamic coefficients using adjoint calculus
- Use sensitivity as indicator for local grid refinement
- Couple indicator to TAU adaptation tool or mesh generation software



CFD Solver

Discretization Issues

Computation of Gradients (FV)

Accurate gradients needed for

- Value reconstruction (upwind)
- Viscous fluxes
- Turbulent sources

Standard gradient construction methods fail on arbitrary meshes

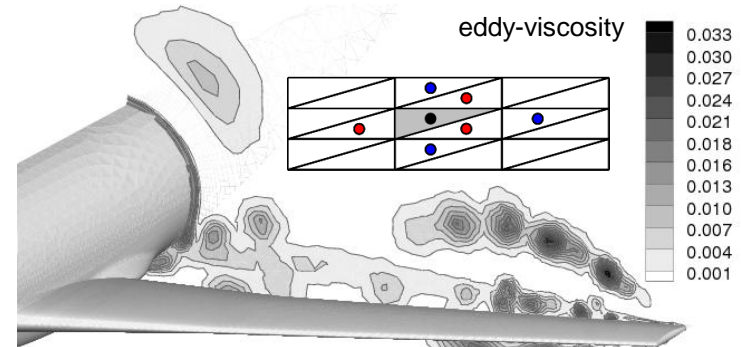
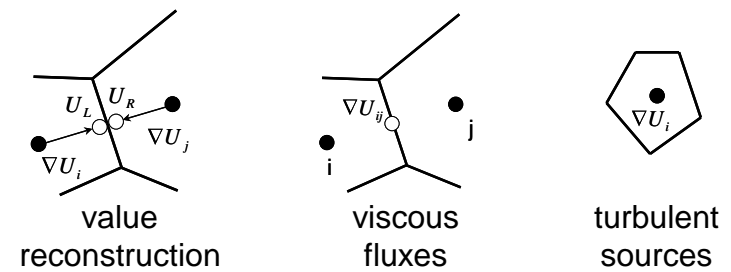
- Unweighted / weighted least-squares
- Green-Gauss
- Averaged & corrected cell gradients on faces

Improvement (e.g. least squares)

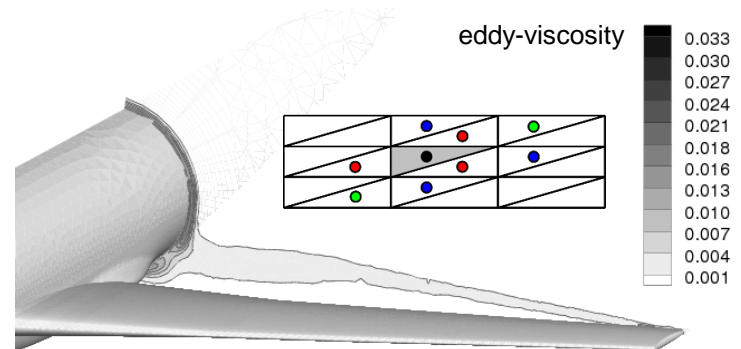
- Enhance weighted stencils to improve condition of linear system

Consequence

- Extend edge-based data structure to provide information that is needed



smart augmentation
least-squares gradients



conditioned smart augmentation
least-squares gradients

Collaboration with B. Diskin (NIA)

CFD Solver

Implicit Methods

Goal

- Reduce stiffness (grid, turbulence)
- Improve robustness and reliability
(**unstructured FV solver TAU**)

Approach (TAU prototype)

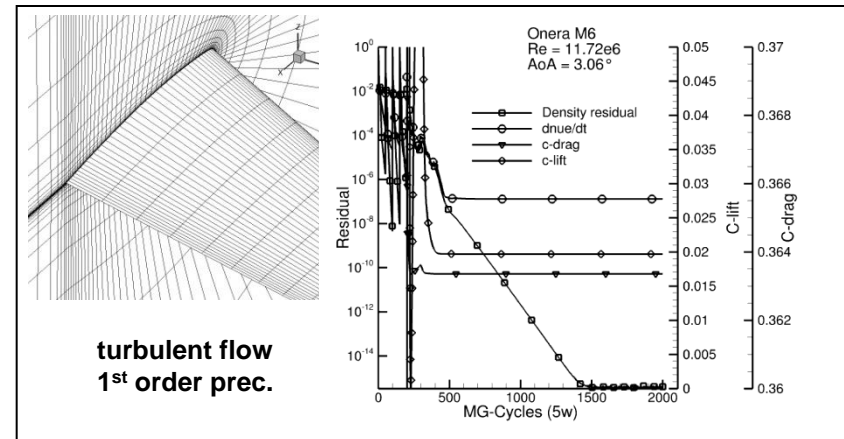
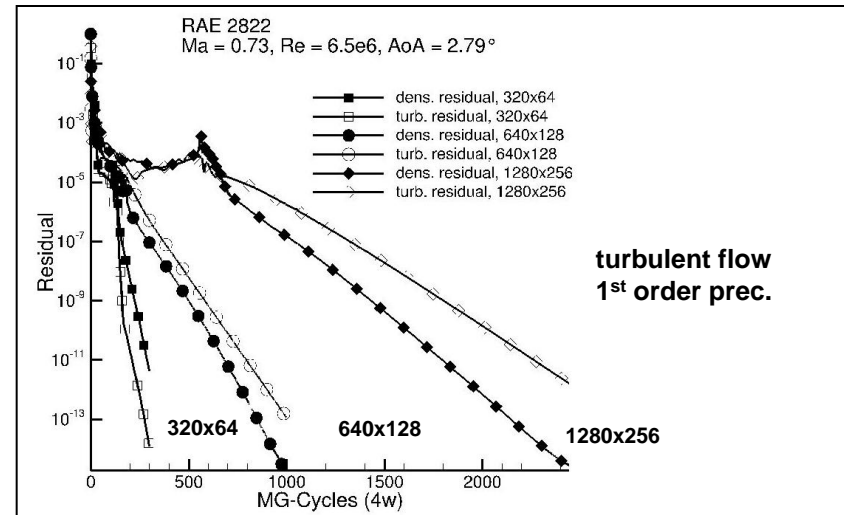
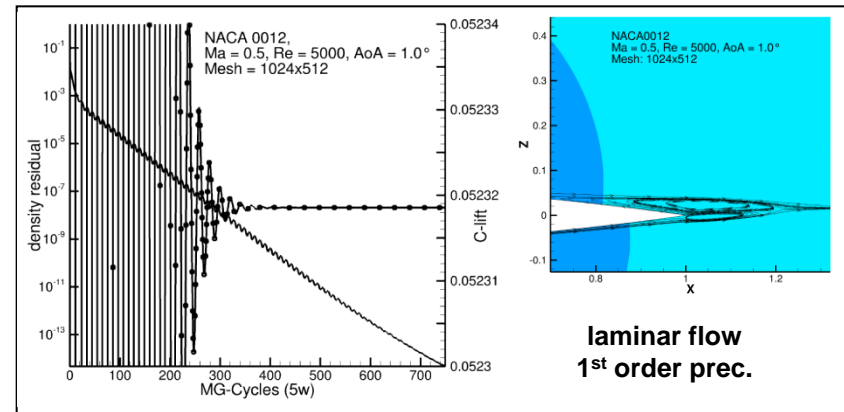
- Preconditioned implicit multistage Runge-Kutta (RK) method as multigrid smoother
- Hierarchy of preconditioners:
(point implicit, line implicit, 1st-order Jacobian)
- Efficient solution of linear systems
- Directional coarsening strategy
- Coarse grid discretization / agglomeration

Open issues

- Treatment of turbulence equations
- Treatment of anisotropic areas in 3D
(e.g. wing nose region)
- Parallelization
- Higher-order discretization



Collaboration with C. Swanson



CFD Solver

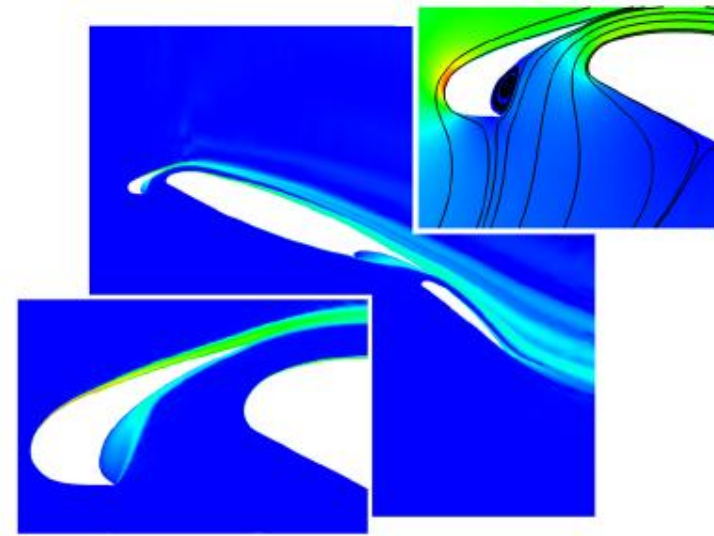
Adaptive Higher-Order DG Method

DLR PADGE Code

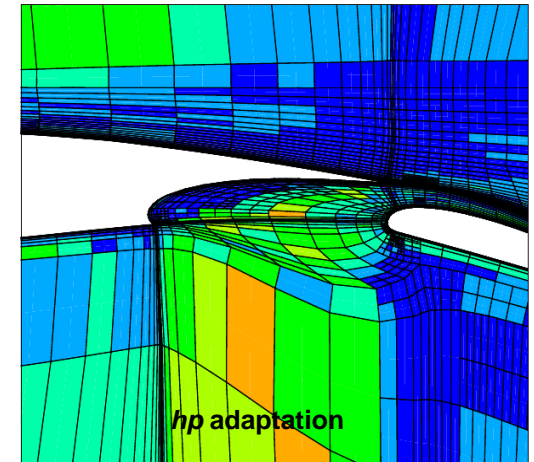
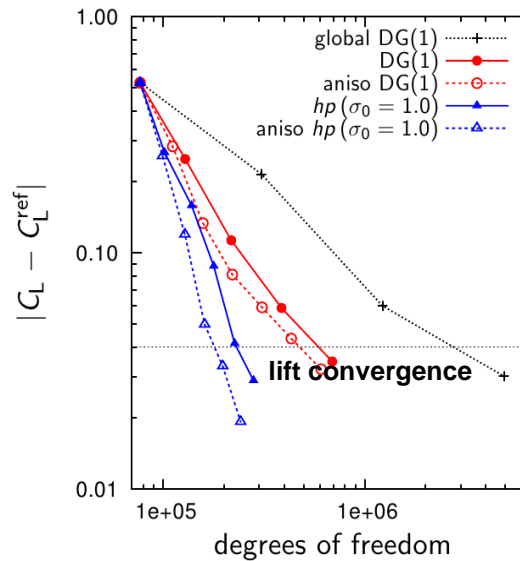
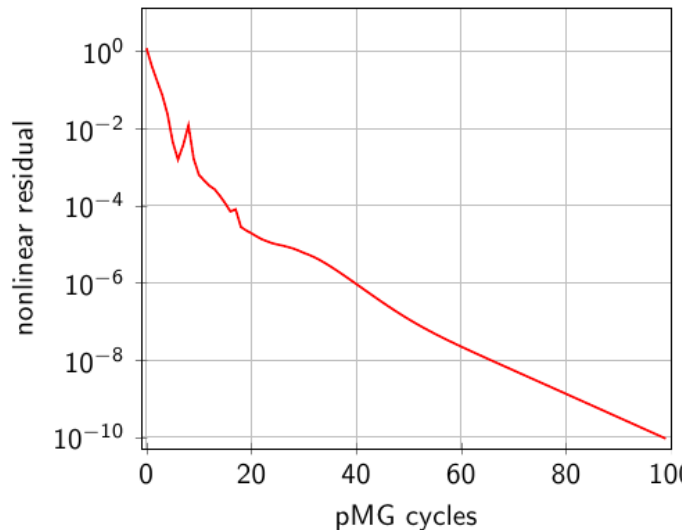
3-element airfoil, L1T2 test case

$M=0.197$ $Re=3.52 \times 10^6$ $\alpha=20.18^\circ$

RANS- $k\omega$, fully turbulent computation



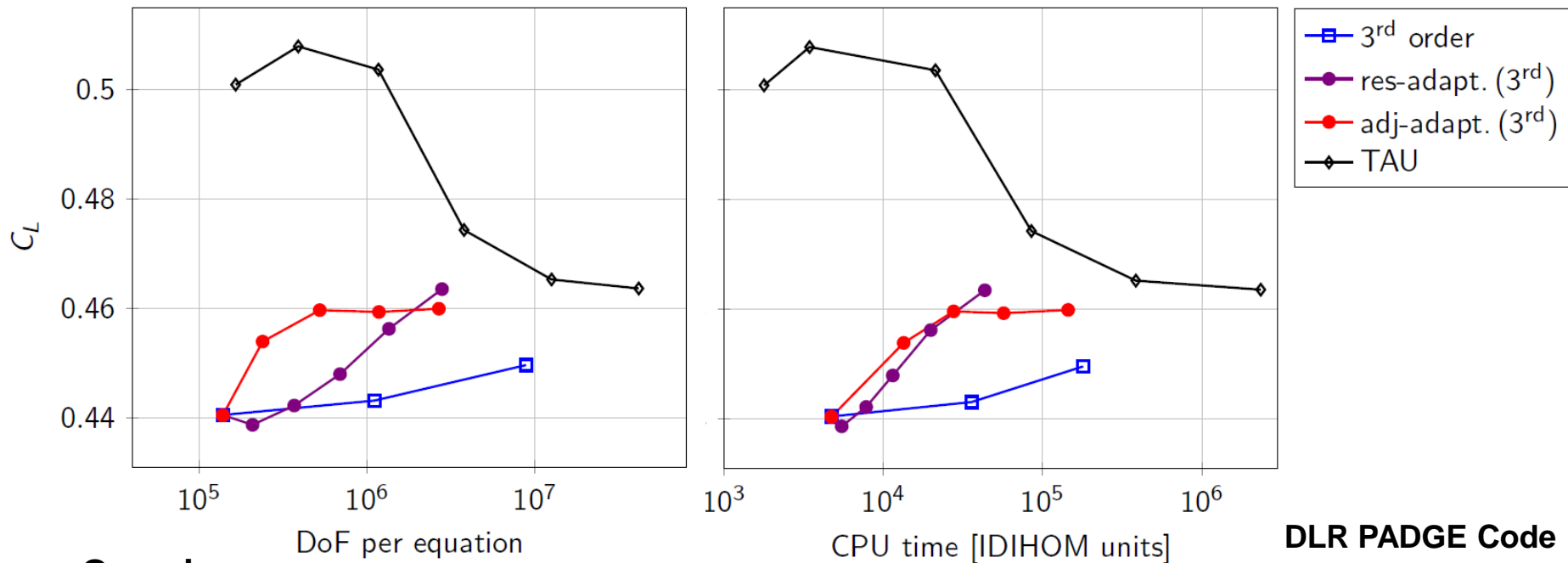
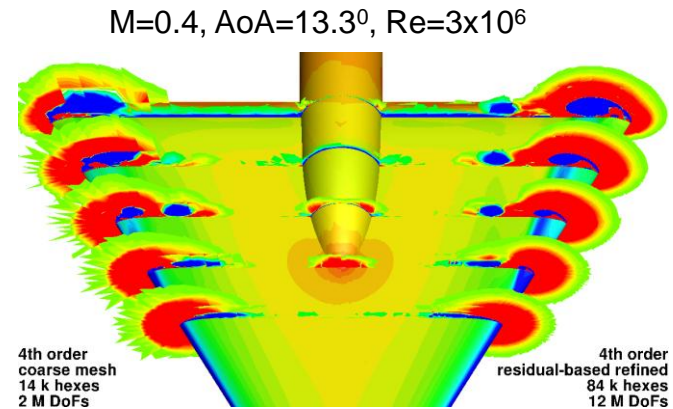
p-multigrid, fourth order solution



CFD Solver

Adaptive Higher-Order DG Method

- Subsonic turbulent flow around VFE-2 delta wing
- Adaptation improves the overall time to solution, in particular if based on an adjoint problem



Open issue:

- Applicability to complex configurations (computational complexity, higher-order boundary representation)



CFD Solver

The Manycore Shift – Facing Massively Parallel Systems

Challenges (in particular for RANS simulations)

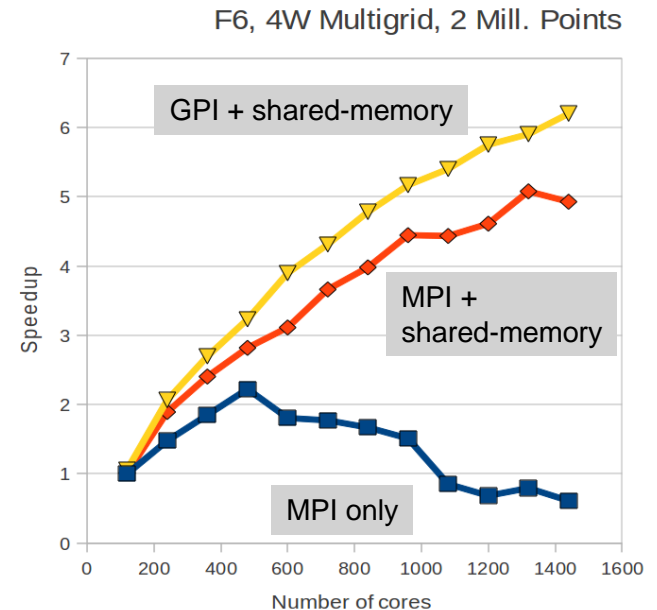
- HPC clusters offers multiple levels of explicit parallelism (*task & data parallelism*)
- Number of mesh points per core drops due to rapid increase in core count
- Classical domain decomposition using one domain per core no longer appropriate because of load imbalances, e.g. due to algorithmic constraints (e.g. “lines”)
- Communication is becoming a bottle neck

Approaches

- Multi-level parallelization allowing for relaxed synchronization, e.g. one domain per chip plus shared-memory parallel processing of domains
- Overlap communication with computation
- Use 1-sided RDMA-based asynchronous communication (e.g. “GPI” instead of MPI)

Goals

- Hide load imbalances and communication to improve (strong) scalability
- Compromise algorithmic vs. parallel efficiency to minimize turn-around time



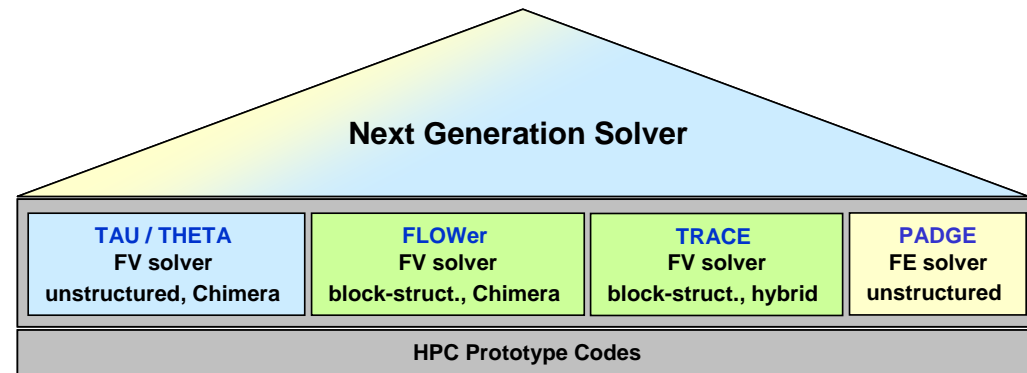
CFD Solver

Activities / Perspective

DLR Next Generation Solver

Objectives

- Data layout driven by
 - Full exploitation of new HPC hardware (multi-level, task & data parallelism)
 - Flexible data structure for allowing enhanced discretization stencils
 - Integration of different discretization strategies (FV, FE, ...)
 - Integration of various meshing strategies (e.g.: overlapping meshes, hanging nodes, grid adaptation, ...)
 - Support of sophisticated solution algorithms
- Modular software design (Use of libraries: post processing, Chimera functionalities, linear solvers, ...)
- **Selection of appropriate numerics on a case-by-case basis**
- Meet increasing user requirements
- Basis for internal and external flows
- **Seamless integration into multi-disciplinary simulation environment (FlowSimulator)**



Maneuver Simulation

Loads Prediction

Current situation

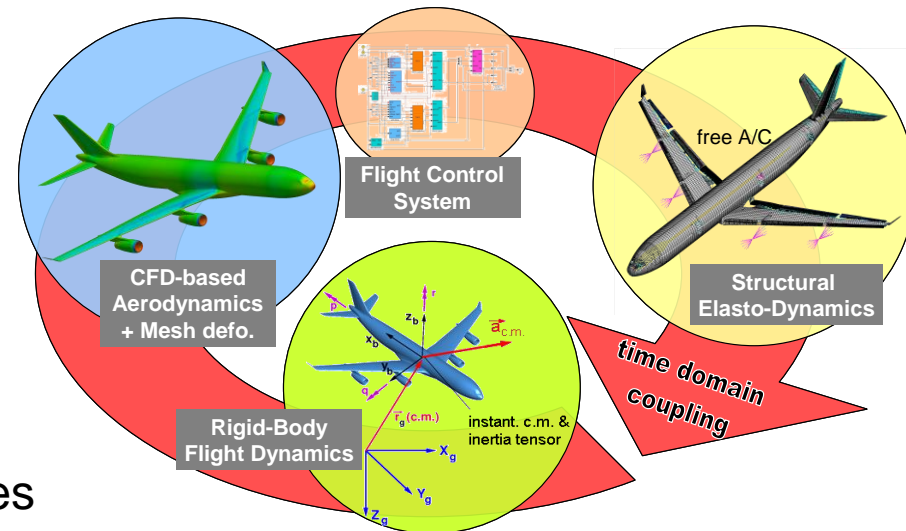
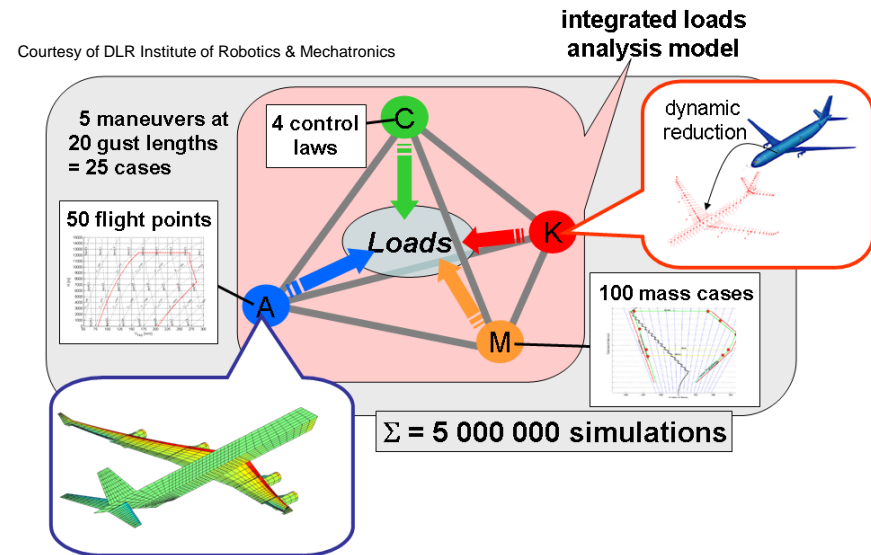
- Loads prediction mainly on low-fidelity methods

Objective

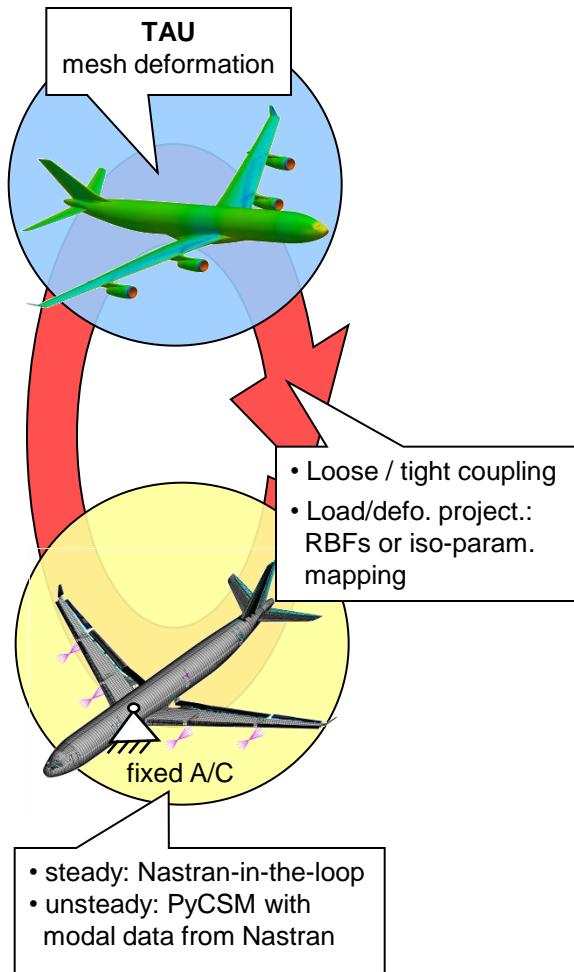
- Accurate maneuver and gust loads analysis for entire flight envelope

Challenges

- Coupling of relevant disciplines for free-flying flexible A/C in time domain based on high-fidelity methods
- Reduced order modeling
- Modeling of moving control surfaces
- Massively parallel simulation environment



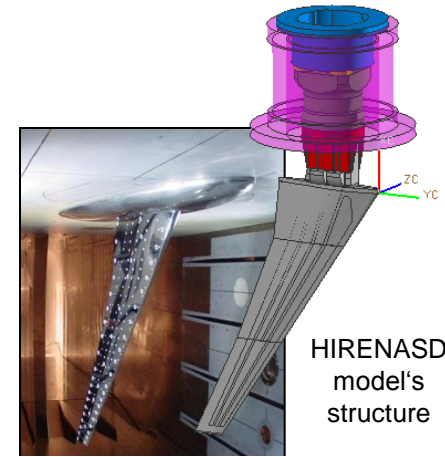
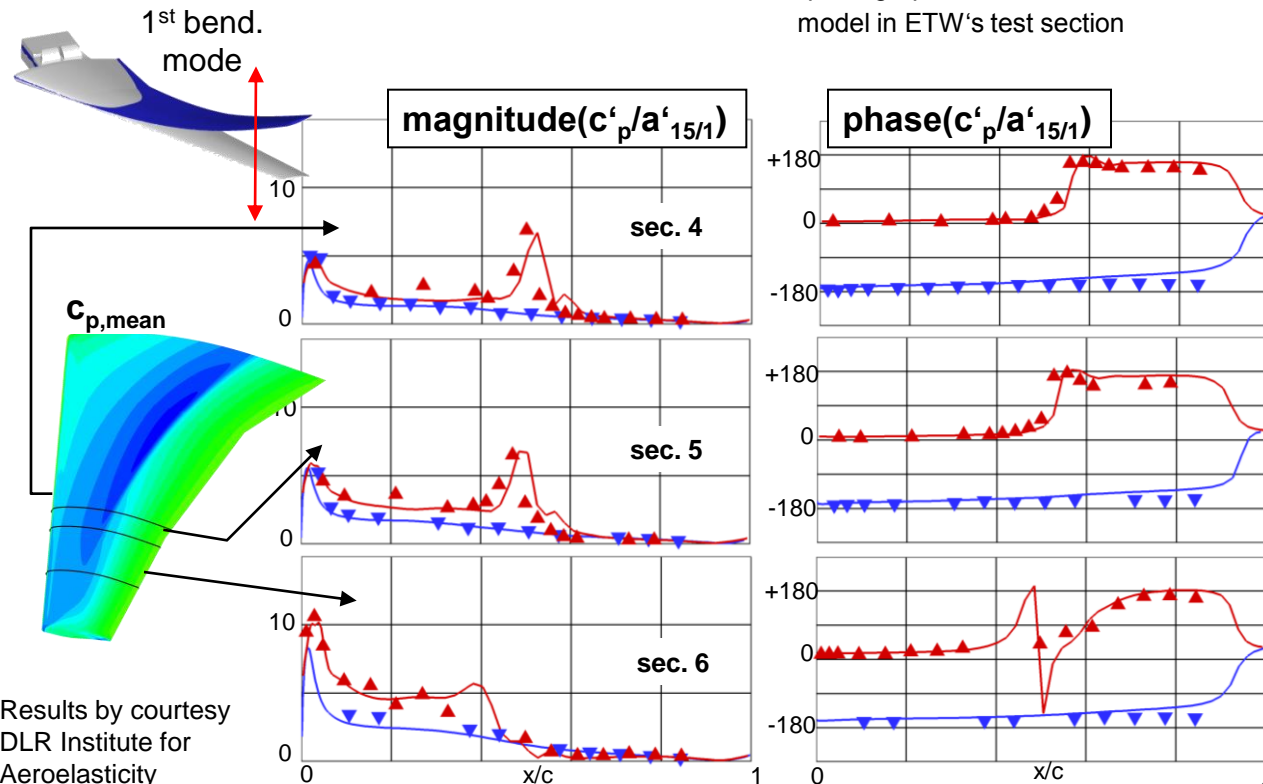
CFD /CSD Coupling – Unsteady Aeroelastics



Example: HIRENASD configuration (AePW)

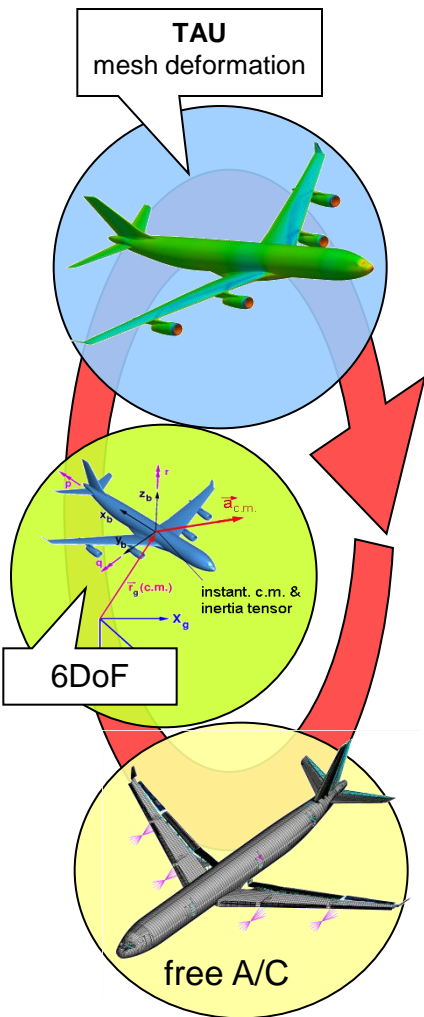
Test 143

- $M=0.8$, $Re=7M$, $\alpha=1.5^\circ$, $f_{exc}=26.92Hz$
- Excitation of 1st bending mode



photograph of HIRENASD
model in ETW's test section

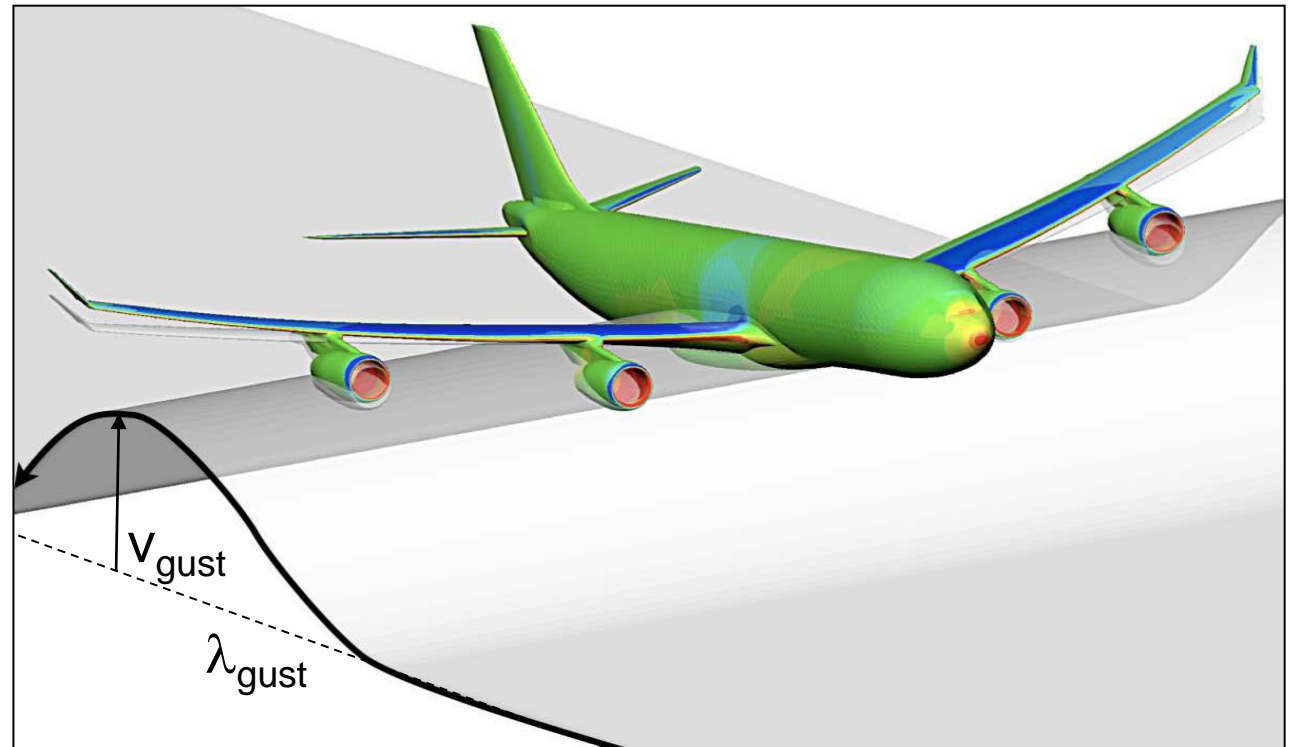
Steps Towards CFD-CSM-FM Coupling



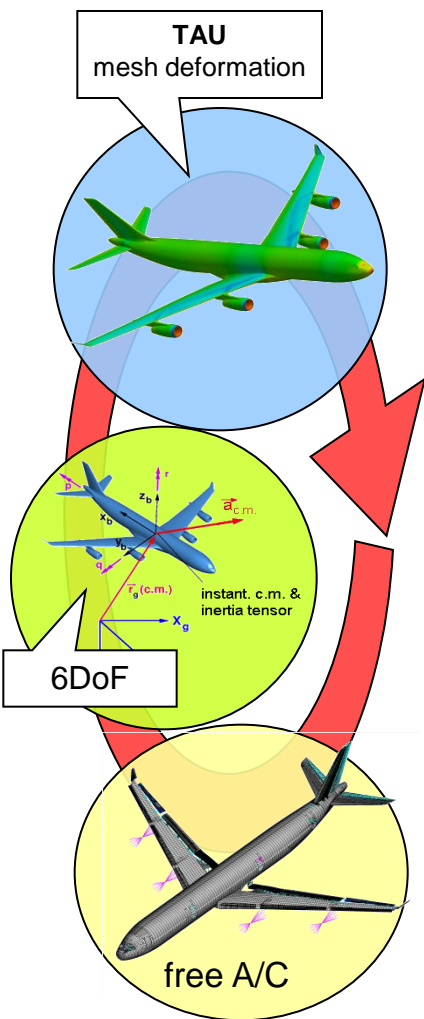
Unsteady example: Gust encounter of flexible A/C

$M=0.82$, $Re=35.3M$, $m=195\text{ t}$, $\lambda_{gust}=60m$, $v_{gust}=15m/s$

- Gust modeled via disturbance velocity approach
- Coupling to flight mechanics (6DoF)
- Coupling to structure

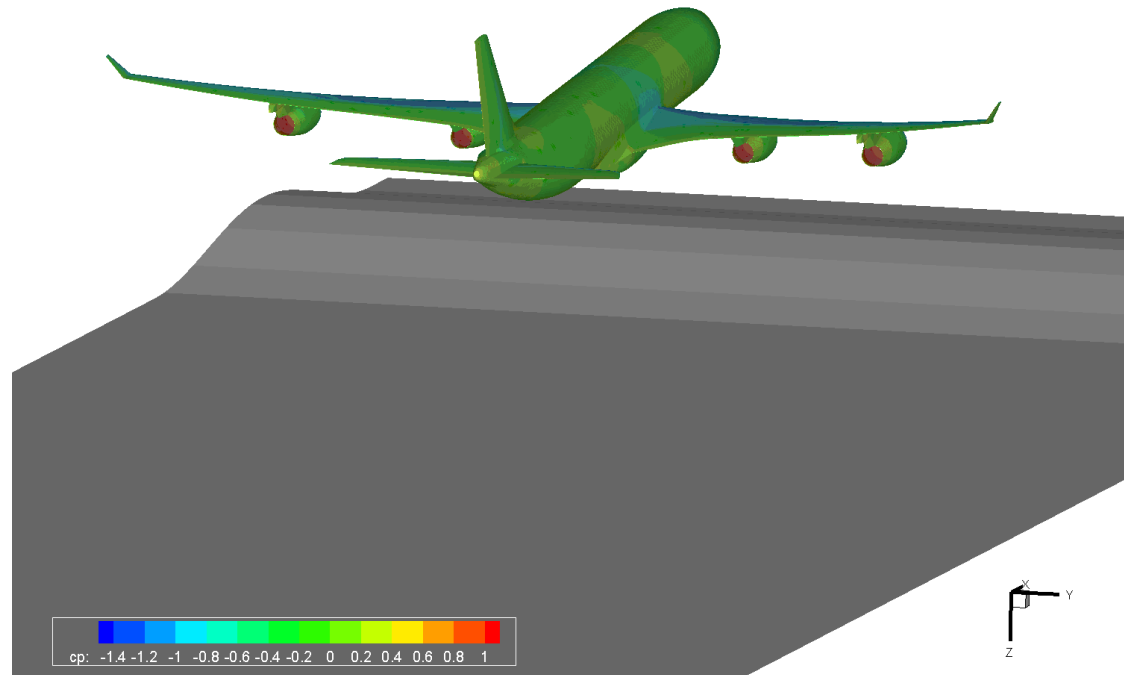
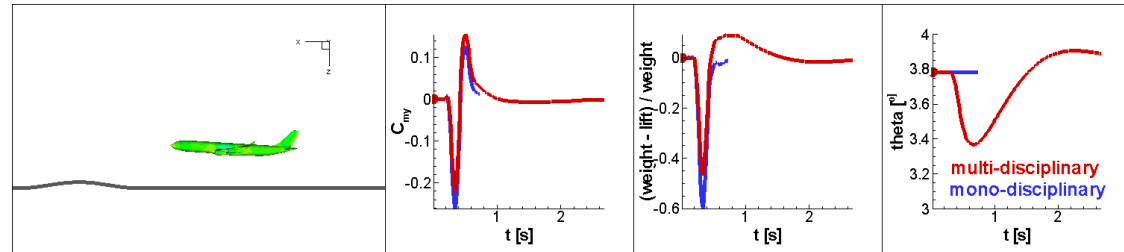


Steps Towards CFD-CSM-FM Coupling



Unsteady example: Gust encounter of flexible A/C (structure; quasi steady)

$M=0.82$, $Re=35.3M$, $m=195\text{ t}$, $\lambda_{\text{gust}}=60\text{m}$, $v_{\text{gust}}=15\text{m/s}$



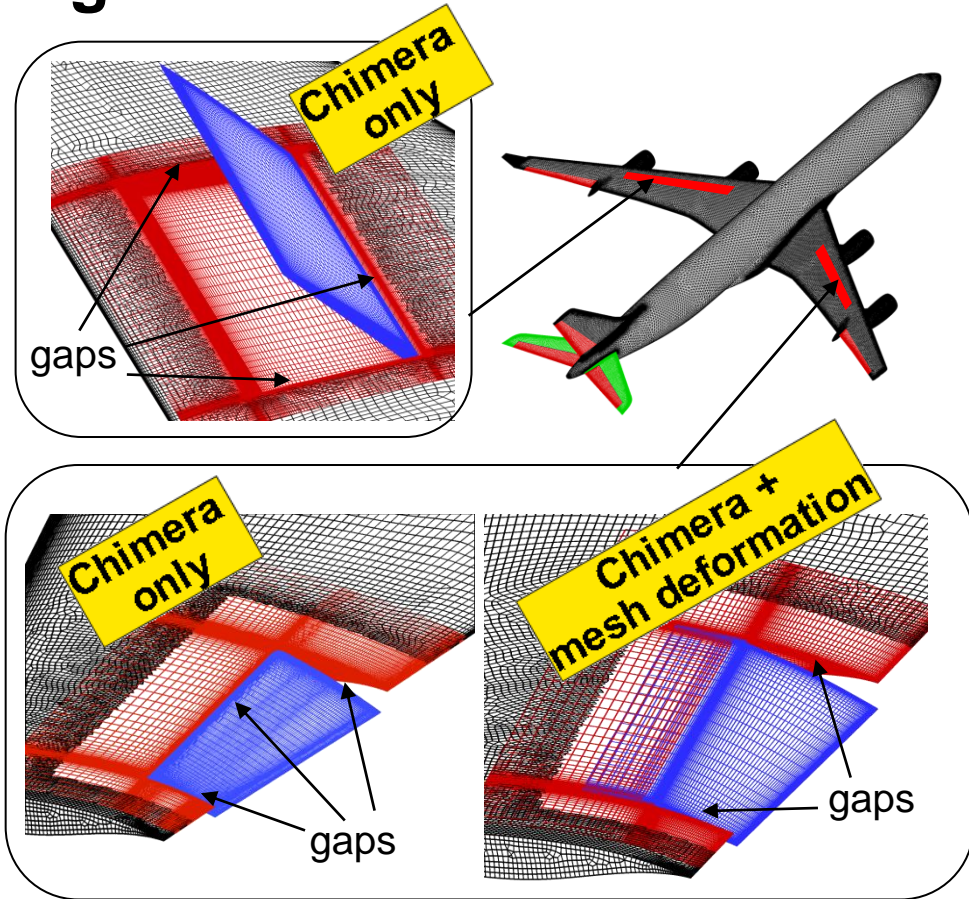
Control Surface (CS) Modeling

Challenge: Moving control surfaces

- Handling of gaps
 - Mesh deformation: small deflections
 - Chimera: waste of grid points for overlap
- Automatism for CS set-up
- Solver robustness
- Flexible A/C configurations

Approach

- Combination of Chimera and mesh deformation
- Improvement of CFD solver with respect to Chimera applications (hole cutting, interpolation techniques, set-up)
- Investment in sliding interface technique



Gust Modeling / Wake vortex Convection

Challenge

- Realistic gust modeling
- Accurate prediction of gust convection or wake vortices

Approach

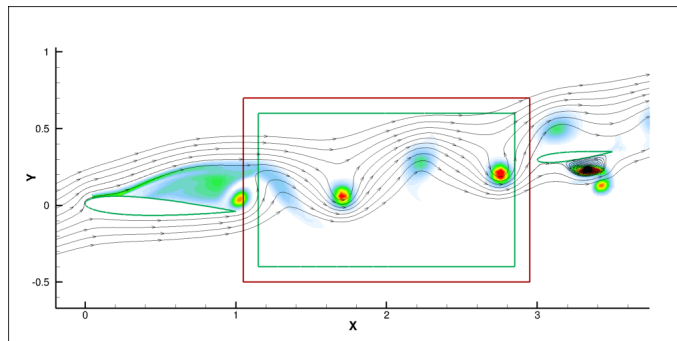
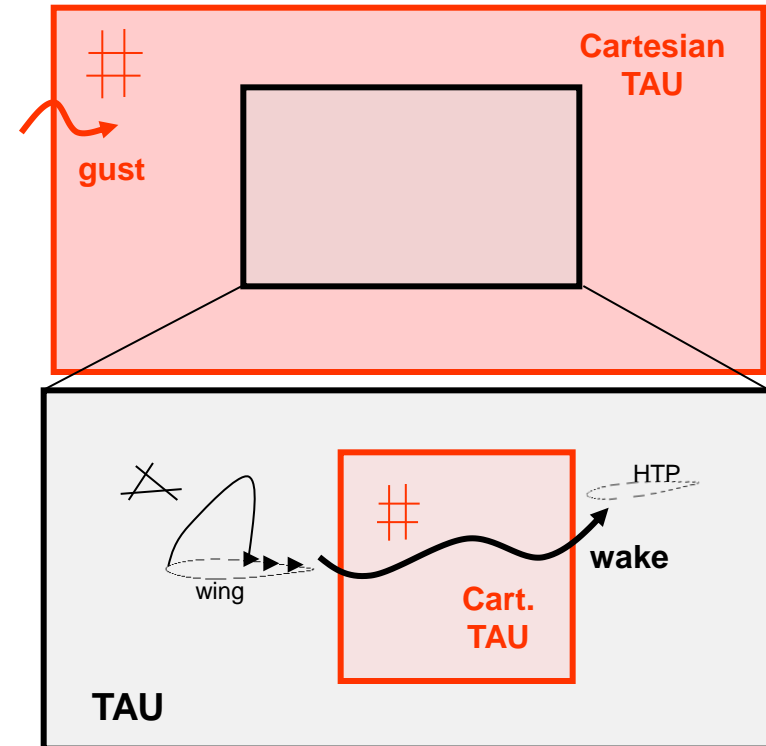
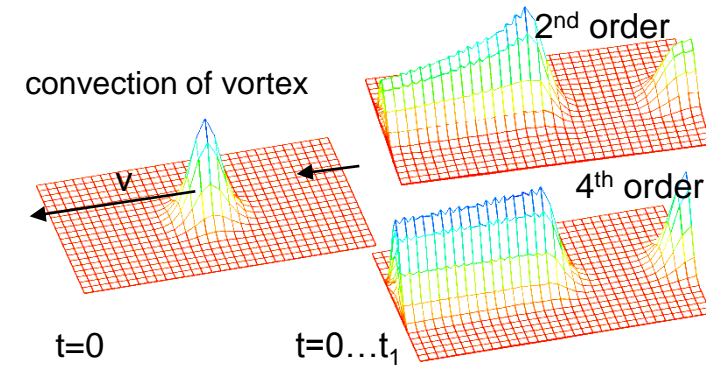
- Coupling of higher-order Cartesian solver (CTAU) to 2nd-order baseline TAU solver

Cartesian TAU

- Off-body solver based on TAU data structure
- Dedicated to Cartesian meshes
- $\geq 4^{\text{th}}$ -order in space (PADE scheme)

Code-to-code coupling

- Chimera-like volume interpolation

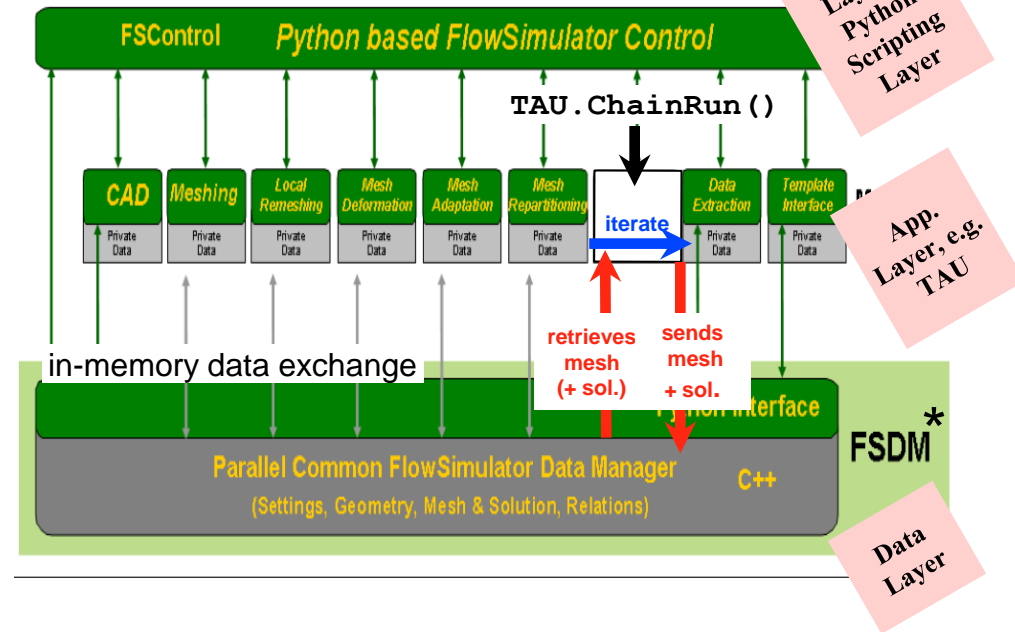


Parallel Simulation Environment

FlowSimulator

Objective: Working horse for multi-disciplinary simulations

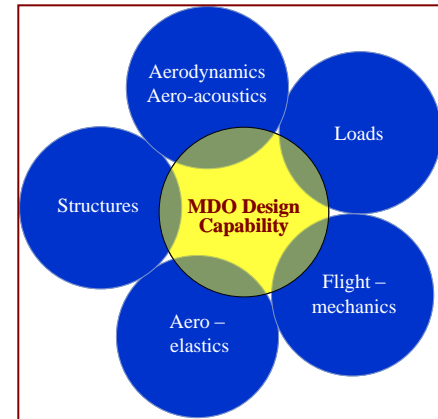
- Kernel jointly developed by Airbus, Cassidian, **DLR**, ONERA, universities, ...
- Designed for efficient massively-parallel in-memory data exchange
- Data exchange via common parallel data structure (FSDM)
 - Easy interchangeability of process chain components
- Python-based scripting layer enables rapid prototyping of tool chains



Multi-Disciplinary Optimization

Current status

- Overall aircraft design capability based on low fidelity models
 - Development of a data model common for all disciplines
CPACS - *Common Parametric Aircraft Configuration Scheme*
- Prototype aero/structural optimization using CFD

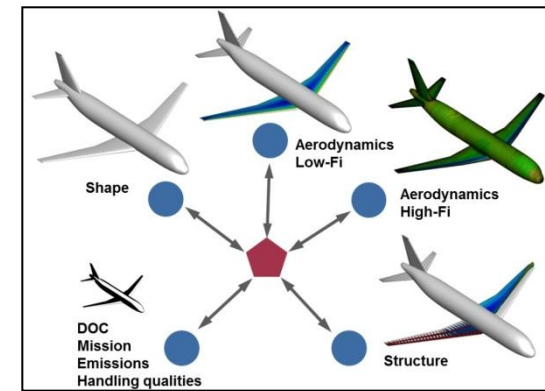


Main objective

- Integrated high-fidelity aero/structural design platform

Challenges

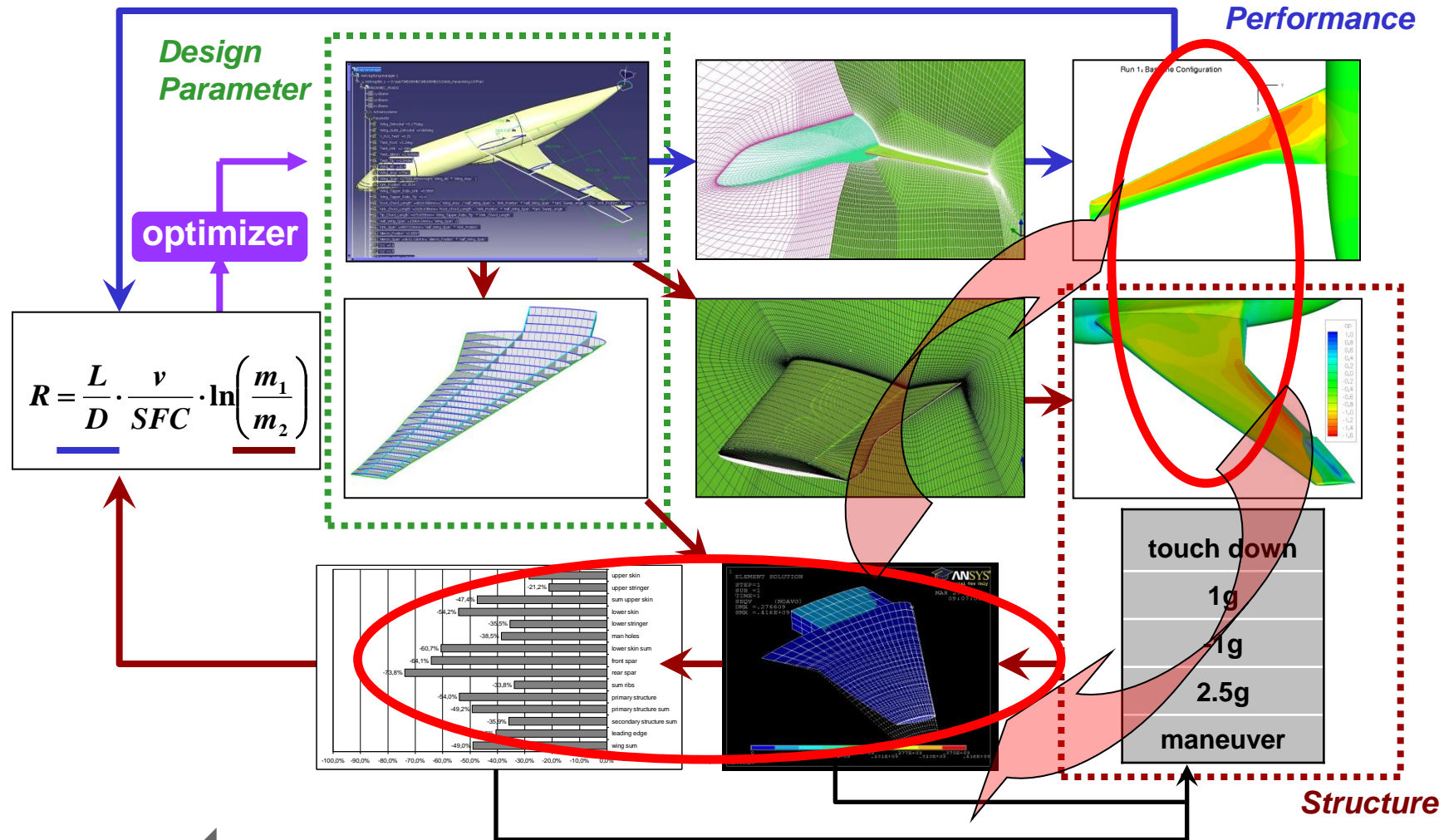
- Efficient multi-level fidelity MDO architecture, combining detailed & overall A/C design capabilities
- Consistent A/C description (CEPACS) for all fidelity levels
- Mix of global (wing planform) & local (airfoil shape) parametrization
- Realistic load cases at appropriate level of fidelity
- Consistent hierarchical structure generator, structural sizing & optimization methods for metallic and composite materials



CEPACS



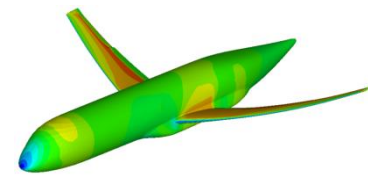
Status: Aero-Structural Wing Planform Optimization



Multi-Disciplinary Optimization

Detailed Design

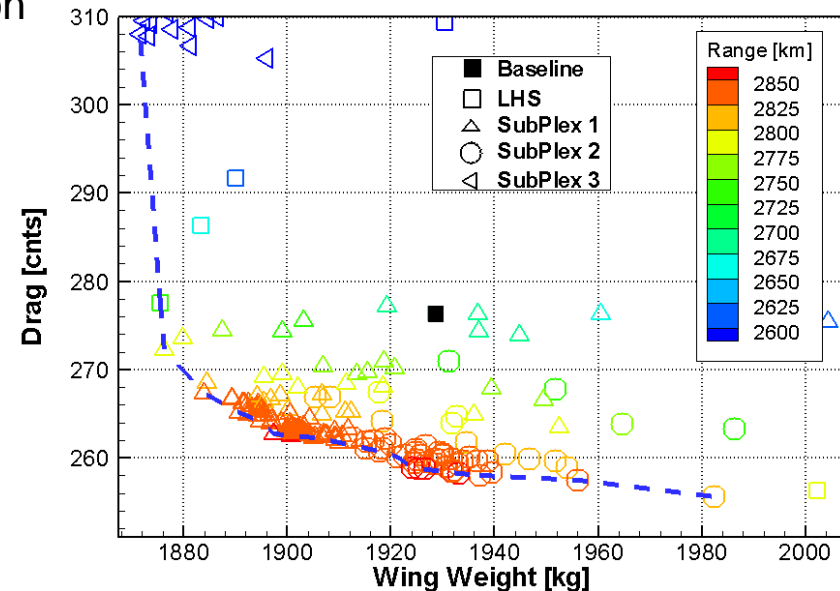
Status: Aero-Structural Wing Planform Optimization



- 7 Design parameters
 - Aspect and taper ratios
 - Sweep angle
 - Twist at 4 sections
- Structure sizing
 - 27 Ribs, 2 Spars, Lower & Upper Shell
 - 4000 nodes

Result:

- Increase the range by 6%
 - Decreasing drag and weight
 - Increasing the taper ratio
 - Increase the span
 - Decreasing the twist law



Time for optimization:

- 213 optimization cycles ~36 days.

Resources used:

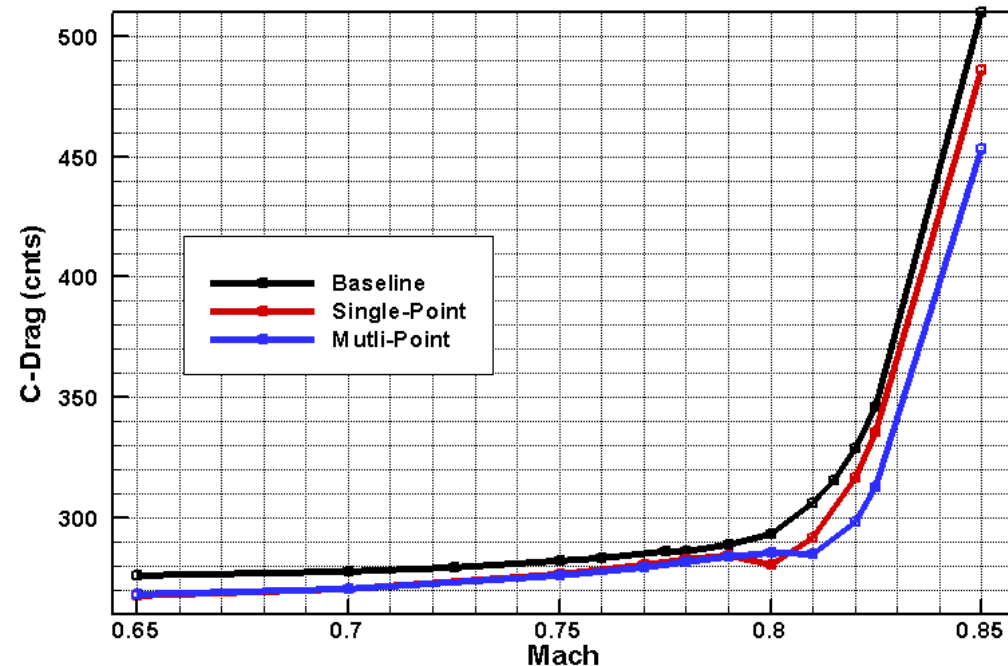
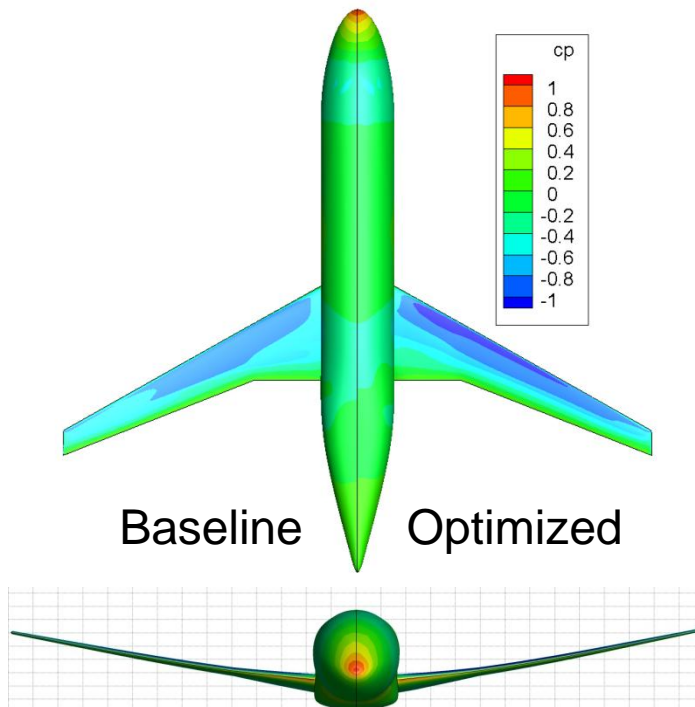
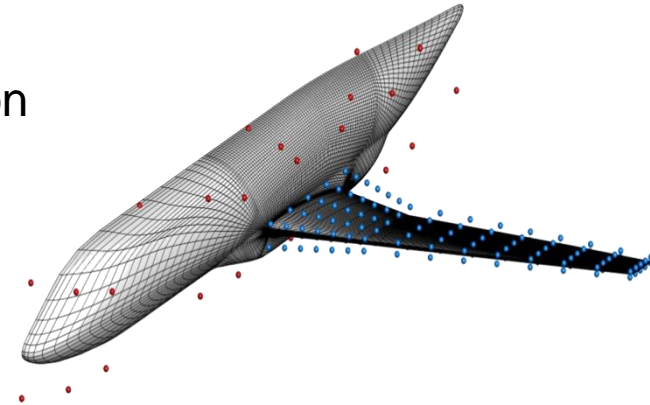
- 24x12=288 cores and 213x20=4260 jobs

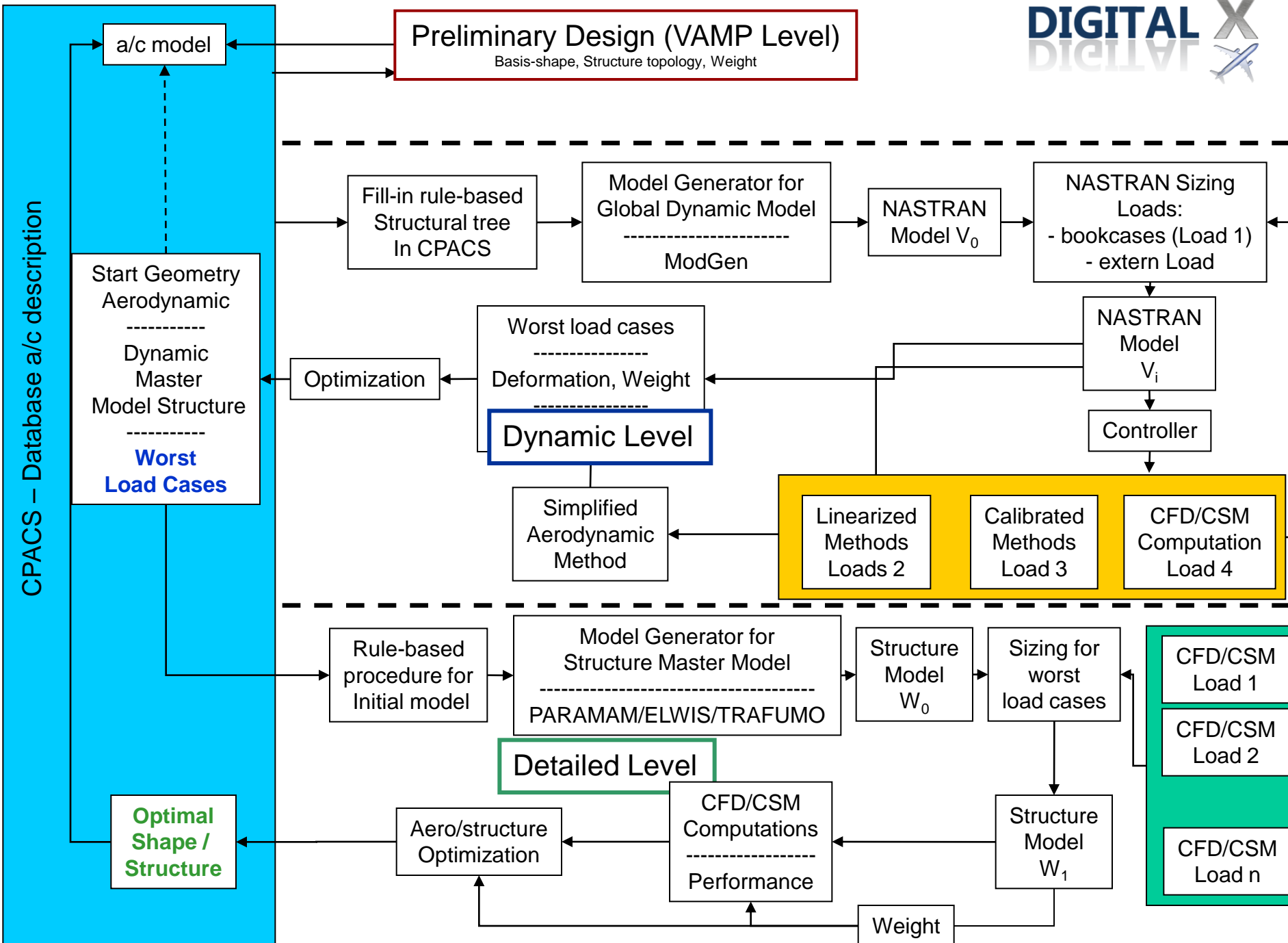
Multi-Disciplinary Optimization

Fluid/Structure Coupled Adjoint for Detailed Design

Discrete adjoint approach for efficient gradient evaluation

- Shape optimizations with 75 design variables
- Aero-elastic deformation considered
- Structure thickness considered as constant
- Single/Multi-point optimizations in viscous flows





Summary

- Digital Aircraft / Digital Product – DLR perspective for numerical simulation (long term vision)
 - Focus of numerical simulation activity at DLR
- DLR project set up: 1st phase 2012-2015
 - Multi-disciplinary project
 - Main goal: **Prototype of integrated MDA/MDO high-fidelity based simulation platform**
 - CFD key enabler, but not the only ingredient
- Dedicated CFD improvements/enhancements
 - Physical modeling (RSM approach)
 - Exploitation of heterogeneous manycore HPC clusters
 - Improvement of solver efficiency & reliability
 - **Layout and prototype implementation of DLR Next Generation Solver**
- Grid generation of high quality grids is still an issue



Summary

Strategic networking to gain full advantage

- Simulation Supercomputing
- Validation Dedicated Windtunnels
- Demonstration Flight Test Capability

Example: HINVA (High Lift INflight Validation)

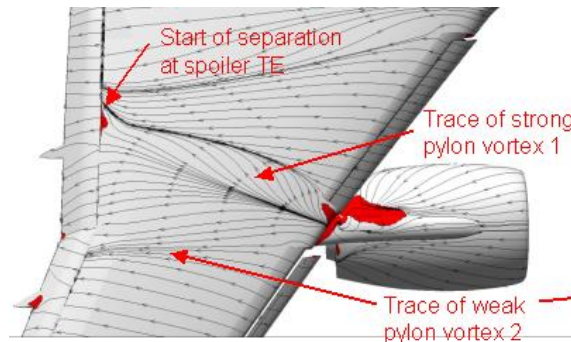
(Project within in the frame of the German Aeronautics Research Programme)



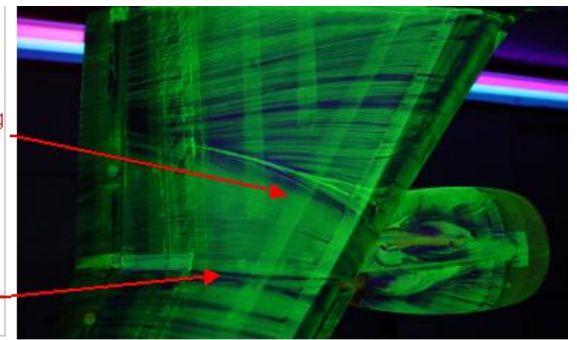
DLR A320-Flight Test A/C



CFD



ETW Windtunnel



Selected references

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